# Mathematics Vocabulary Dictionary (Reception – Year 6)

Welcome to the MathSphere Vocabulary Dictionary which explains the meaning of almost all the words and terms to be found in the English Primary Maths Curriculum. Some terms stand alone and are defined within their own entry in the dictionary. Others are best explained in the context of a major topic and the user is referred to the title of the major topic where the relationship between the required entry and related entries is to be found. For example, words such as '**metre'**, '**kilogram'** and '**litre'** will be found under the major topic of '**Metric System**'.

Many of the simplest of words have been included, even though their meaning is obvious to any adult, because their inclusion provides us with the opportunity to explain the contexts in which these simple words are used. The word 'divisibility', for example, is introduced early on to simply mean the process of dividing one number into another with no remainder, but later children will use it for divisibility tests which require a much greater facility with number.

The numbers following each entry in brackets give the year in which the word is expected to be first introduced to the child. This may be very ambitious target for many children!

Historically, mathematics arose originally from an attempt to try to describe and measure the world around us. This may no longer apply for mathematical geniuses who talk a language 99% of the population are not privy to, but at the age of the children we are concerned with, it is as true today as it always was. Recognizing this fact helps us to help children learn the vocabulary they need as it is all around them. There is always something that is larger, smaller, heavier than something else. The world is full of symmetrical objects. We use hours, minutes, seconds, days and months all the time. The important thing is to use them with the children at every opportunity, slowly building their knowledge and understanding. Children love new words – don't be afraid to use them. Good luck!

#### 12-hour clock (5)

A clock that shows the time on a **12** hour face and also the way of writing time followed by **a.m.** or **p.m.** e.g. **11.45** p.m. Although we often omit the a.m. and p.m. when it is clear whether we are referring to before noon or after noon, these should be included if there is any possible doubt.

A.m. stands for the Latin phrase 'ante meridiem' (before noon) and p.m. stands for 'post meridiem' (after noon). Noon is therefore neither a.m. nor p.m. Midnight is also confusing since it is both the beginning and end of the day. To avoid doubt it is better to say **12.00 noon** and **12.00 midnight** as appropriate. In cases where it could be crucial if it was not clear on which day the midnight fell such as legal contracts, insurance policies, airline flights, **12.00 midnight** is mostly avoided and **11.59 p.m.** and **12.01 a.m.** are used instead.

All these are good reasons for using the **24-hour** clock when any confusion could arise. Historical note. It is interesting to notice that clocks that display the time in Roman Numerals normally use **IIII** instead of **IV** for the number four. This is said to be because Henry VIII once designed a clock and used IIII instead of **IV** by mistake. When he gave the design to his clock makers they were so terrified of him that no-one dared to point out his error and they made the clock using **IIII**. This has since become a tradition.

#### 24-hour clock (5)

The method of writing time using four digits with midnight at the beginning of the day being 00.00 (the separator between the hours and the minutes is not necessary, but is often included for clarity). If the hour is below **10** a leading zero is included as in **03.40**, **09.00** etc. Times up to **12.00** are obviously before noon and times from **12.00** to **24.00** are after noon (although **24.00** itself is nearly always written as 00.00 to indicate the start of a new day).

No a.m. or p.m. are used as they are now redundant. Whilst the **24**-hour clock removes much of the confusion of the **12-hour** clock, there is still the problem of **00.00** – does this refer to the midnight at the beginning of the day or at the end. In cases where it could be crucial if it was not clear on which day the midnight fell such as legal contracts, insurance policies, airline flights, **00.00** is mostly avoided and **23.59** and **00.01** are used instead.

In August **1852**, Charles Shepherd built and installed his Galvano-Magnetic clock at the Royal Greenwich Observatory. This was a true **24** hour clock, built as a normal round **12-hour** clock, but with **24** numbers.

#### 2D (4)

See the major topic TWO DIMENSIONAL SHAPES

#### 3D (4)

See the major topic THREE DIMENSIONAL SHAPES

# A.M. (3)

See '12-hour clock.'

### Abacus (Plural 'Abaci') (1)

**a)** A calculating device from the east constructed of beads sliding on rods. There were several types in use over the centuries, one of which had a pair of beads and a group of five beads on each wire, the pair and group of five being separated by a wooden strip:



**b)** In classrooms today a simpler type is used in which children drop beads onto rods. The process of grouping ten beads to make one bead in the next column to the left or decomposing one bead to ten beads in the next column to the right can be clearly seen.



This abacus shows 7 256.

To add, say, **1 273** to this number, add put three more beads on the units wire, making **9**. Put seven more beads on the tens wire, making **12** altogether. As this is more than nine, remove ten from this wire and add one more to the hundreds wire, making **3**.

Add two more beads to the hundreds, making **5**. Finally, add one more to the thousands column, making **8**. The final total, **8 529** is now shown thus:





#### Afternoon (R)

The period following on from noon.

#### Altogether (R)

The result of an addition sum as in, 'Tom has four cakes, Julie has three. They have seven cakes altogether.' This raises the interesting point of the abstraction of numbers from real situations. Four plus three is seven whether it seven cakes, seven cars or just plain seven. It takes a while for the abstraction from working with objects to working with pure numbers to occur. In fact, the process needs to be repeated later such as when dealing with negative numbers. Children may be very proficient with adding and subtracting positive numbers, but when they move on to adding and subtracting negative numbers they often need a practical example such as temperatures or bank balances to cling to.

#### Alwavs (1)

The idea that some things always happen. 'The sun rises ever day.' 'Mrs Jones always takes the register on school days.'

#### Amount (3)

Used first to indicate an amount of money - the total of all those coins and notes. Later used in all sorts of ways to indicate the amount of a rotation, the amount of liquid in a measuring cylinder etc.

# Analogue clock/watch (2)

See Digital/Analogue

#### Angle - greater/smaller angle (3)

The most important concept children need to learn about angles is that an angle is a measure of a rotation and any way we have of referring to an angle (half turn, right angle, 50° etc) is simply a reference to this rotation. One angle is therefore greater or smaller than another if it represents a greater or smaller rotation.

There are many things in the real world that rotate and that children are very familiar with - the hands of a clock, the needle on weighing scales, the steering wheel of a car etc, so there is plenty to see and discuss.



#### Angle measurer (4)

A device for measuring angles. The most familiar is probably the protractor, but even this comes in two versions – the **180<sup>°</sup>** and the **360<sup>°</sup>** types. There are other types of angle measurers involving two arms, one of which remains stationary while the other rotates.

#### Anti-clockwise (2)

Rotating in the opposite direction to the hands of a clock. Later this type of rotation will be formalized in describing transformations, so it is important for children to have a good understanding of the concept of rotation and anti-clockwise at primary level.

#### Apart (R)

Not connected.

#### Approximate (3)

Often used in estimating: 'The approximate distance from the classroom to the school gate is fifty metres.' 'An approximate value for pi is 3.'

#### Approximately (3)

Similar to 'Approximate': 'The pupil was approximately five minutes late.'

#### Approximately equal to ( $\approx$ ) (5)

It is the sign that is new here. By now children should have a good idea of the concept of 'approximate'. How close two things need to be to be approximately equal to each other is a matter of judgement which needs refining over the years. We would probably agree that 48 + 51 ≈ 100, but would we agree that **39 + 40 ≈ 100** ?



# Arrow (1) a) A simple arrow used to point to positions on a number line. b) The arrow shape. See the major topic on TWO DIMENSIONAL SHAPE. As many as (5) Used in questions on proportion. E.g. 'In this pattern there are as many circles as squares' Ascend (3) To go up as in ascending a ladder in the game of snakes and ladders. Ascending order (5) Numbers written in order with the smallest first. August (2) See the major topic TIME. Autumn (1) One of the four seasons. The main idea for children to understand is that the seasons are cyclic; it is impossible to say which is the first season and which the last. Average (6) One of the three terms: mean, median or mode. When used in everyday language, 'average' nearly always means 'mean'. Axes (3) Plural of axis. Axis (3) One of the lines on a graph on which the scale is placed. They should always be labelled with a suitable phrase such as 'time' or 'days of the week'. When no particular units are involved, the horizontal axis is normally labelled the 'x-axis' and the vertical one the 'y-axis'. Axis of symmetry (5) A line passing through the middle of a shape with reflective symmetry so that the half on one side is a reflection of the other half in the line. Often called the 'mirror line' or 'line of symmetry'. Balance (R) A weighing balance, normally the type with two pans, one for the weights and one for the object being weighed. **Balances** (R) a) Refers to the situation when the mass in one pan of a balance is the same as the mass in the other and the pans are level.

**b)** In later life refers to the situation in which an equation balances when the value of the left side is equal to the value of the right side.



#### Beside (R)

Used to indicate the relative position of two objects. Also used to draw attention to consecutive numbers on the number line.

#### Between (R)

Used to indicate the relative position of three objects, one being between the other two. Also used to draw attention to consecutive numbers on the number line.

#### Biased (6)

Used when something is not considered 'fair'. Mechanical devices that are used to generate random numbers fairly are considered biased when the numbers produced differ considerable from those expected over a long run. For example, if a normal dice is thrown we would expect roughly the same number of ones, twos etc if the dice were thrown thousands of times. A dice may be made biased by drilling a small hole in one face and inserting a small, but heavy, weight into the hole. This face will tend to land on the underside of the dice more often than is 'fair' and the opposite face will therefore show more often than it should.

Similarly a spinner may be biased by making some of the edges longer or shorter than others. A roulette wheel may be biased by sloping it slightly.

A survey may also be biased and its results therefore suspect. For example, if you were to stand in a high street between **10.00 a.m**. and **1.00 p.m**. on a Thursday and ask people passing which way they would vote in a general election, you would not obtain a good indicator of how the nation generally would vote as your survey would be biased towards retired people, young mothers with babies and so on. You would not be able to interview many people who worked in an office or factory during normal working hours.



#### Birthday (R)

Putting dates like birthdays and Christmas Day on a calendar helps to give children an understanding of how the calendar works and the fact that it is cyclic. On non-leap years, birthdays occur one day later each year (two days for a leap year). This is because there is a remainder of one when **365** is divided by seven.





#### Capacity (2)

The amount that a container will hold. Measured in the imperial system in litres, millilitres or cubic metres and in the imperial system in pints and gallons.

#### CARDINAL and ORDINAL NUMBERS

Many people are not aware that we use numbers in two completely different ways. When we use numbers in a cardinal sense we are referring to their actual values. This may be in an abstract sense such as **5** plus **3** equals **8** or in a measurement sense such as when referring to **4** litres of milk, a height of **150** metres or a speed of **40** Km per hour. In using numbers in the cardinal sense it is meaningful to perform operations on the numbers such as six eights are forty eight, three litres plus six litres is nine litres, a car covering **160** Km in **4** hours has an average speed of **40** km/hr.

When we use numbers in an ordinal sense we are just using them to refer to the order in which things are placed and it makes little sense to perform operations with them. In this sense, one becomes first, two becomes second, three becomes third and so on. The gold medal is given to the athlete who crosses the line first. It generally makes no sense to add up the positions in a race, for example, and conclude that a third place plus a second place is equal to a fifth place. There is an exception to this and that is when sports people are competing as a team and the <u>average</u> positions are used to determine which teams get the medals. In this case the ordinal numbers indicating finishing positions are then used in a cardinal sense.

Eg. In a cross country race the following positions were achieved by members of three teams:

Name	Team	Position
J Peters	В	3 <sup>rd</sup>
A Cooper	Α	6 <sup>th</sup>
M Kilroy	В	12 <sup>th</sup>
H Corbett	С	18 <sup>th</sup>
L Young	С	20 <sup>th</sup>
T Fredericks	В	<b>22<sup>nd</sup></b> Here the numbers are used in an ordinal sense.
R Williams	Α	27 <sup>th</sup>
G Friedman	В	29 <sup>th</sup>
K Lipman	С	35 <sup>th</sup>
G Davenport	Α	38 <sup>th</sup>
A Sandel	Α	40 <sup>th</sup>
S Town	С	44 <sup>th</sup>
hich team performed	heet based on th	oir finishing position?

Here the numbers are used in a cardinal sense.

Which team performed best based on their finishing position?

Find the average of the positions of the members of each team:

Team <b>A</b> :	Average =	· (6 +	27 +	38 +	- 40) ÷	· 4 =	27.75
	-					-	

- Team B: Average =  $(3 + 12 + 22 + 29) \div 4 = 16.5$
- Team C: Average = (18 + 20 + 35 + 44) ÷ 4 = 29.25

Team B therefore performed the best of these three teams.

Other uses for ordinal numbers include house numbers, receipt numbers and a person's position in a queue such as in a doctor's surgery or at a deli counter.

### Carroll diagram (3)

See Venn and Carroll Diagrams.

#### Centilitre (6)

One hundredth of a litre. See the major topic METRIC SYSTEM for more details.

#### Centimetre (2)

One hundredth of a metre. See the major topic METRIC SYSTEM for more details.





#### Circumference (6)

The distance around the outside of a circle. Approximately three times the diameter ( $\pi$  = 3.14159... times to be more precise). See '*Circle*'.

#### Classify (4)

Group together according to certain rules. Shapes may be classified according to the number of sides or faces, toys may be grouped according to colour and numbers may be grouped according to whether they are multiples of seven, prime or factors of sixty, for example.

Multiple classifications are possible such as finding numbers that are prime and factors of sixty. These may be illustrated on a Carroll or Venn diagram.

#### Clear key (5)

This is a confusing term as there are normally two clear keys on a calculator, one that clears the whole calculator as though you had just turned it on and one that clears the last entry so that small mistakes may be corrected without having to re-type a whole column of number, for example.

The key that clears the whole calculator is often called the 'All Clear' key and is labeled 'AC', but is sometimes labeled just 'C'. The key that clears the last entry is sometimes labeled 'CE' but is sometimes also labeled just 'C'. To confuse matters further, on some calculators one key (which is often labeled ' $C \rightarrow CE'$  or similar) is used for both. One press clears the last entry and two presses clear the whole calculator.

It really is time manufacturers standardized these two function as AC and CE or something equally clear. Until that time I am afraid you will just have to read the instructions to see which key does what.



#### Clock (R)

A device for telling the time. There are two types: analogue clocks and digital clocks. Analogue clocks are the older type with a circular numbered dial over which the hands move. Digital clocks are the modern type with a panel showing just numbers.





**Analogue Clock** 

Digital Clocks can show <u>12 hour</u> or <u>24 hour</u> time.

**Digital Clock** 

Clockwise (2)

Rotating in the same direction as the hands of a clock. Later this type of rotation will be formalized in describing transformations, so it is important for children to have a good understanding of the concept of rotation and clockwise at primary level.

MathSphere dictionary for teaching assistants											
Closed (4)											
A shape (often a polygon) that encloses a space, i.e. has a definite inside and outside.											
								\			
						2	_				
	-										-
Closed shap	e							Ope	en sn	ape	
Coin (R)											
One of the system	ofco	oins ir	ו eve	ryday	use.	It is	impo	rtant	for ch	hildren	to learn that coins have value
irrespective of thei	r phy	sical	sıze,	colou	r etc.	•					
Column (2)											
Rows and column	s as ι	used	in an	array	such	n as a	table	e squ	are.	Colum	ns run from top to bottom like the
columns in the old	Gree	ek or	Rom	an bui	liding	s; ro\	vs ru	n troi	n left	to righ	It as do the seats in a cinema.
_											
Column	1	2	3	4	5	6	7	8	9	10	
	2	1	6	Q	10	12	11	16	10	20	
	2	4	0	0	10	12	14	10	10	20	
Pow	3	6	9	12	15	18	21	24	27	30	
ROW		<b>†</b> °	10	10		0.4			0.0	10	
	4	8	12	16	20	24	28	32	36	40	
	5	10	15	20	25	30	35	40	45	50	
	_										
	6	12	18	24	30	36	42	48	54	60	
	7	14	21	28	35	42	49	56	63	70	
	8	16	24	32	40	48	56	64	72	80	
	9	18	27	36	45	54	63	72	81	90	
	10	20	30	40	50	60	70	80	90	100	

MathSphere dictionary for teaching assistants								
COMPARATIVE and SUPERLATIVE Mathematics is full of interesting vocabulary and a good knowledge of how it all works makes our study of mathematics all the more interesting and precise.								
People often use adjectives to describe objects, but sometimes use them incorrectly when comparing one object with another or others.								
Most adjectives have a comparative and superlative form. The comparative is used when comparing two objects and the superlative when comparing three or more objects. It is important to teach children this difference early on.								
E.g. <u>Adjective</u> <u>Comparative form</u> <u>Superlative form</u> big bigger biggest wide wider widest tall taller tallest								
Correct sentences: Graham is bigger than his brother. (Comparing two) Mary is the tallest in her class. (Comparing more than two)								
Incorrect sentences: I measured the height of Massoud and Reza. Reza is tallest. Josephine has the greater amount of pocket money in her class.								
This system can be extended to comparisons of groups. The trick is to think of a group as one object.								
Correct sentences: We measured the masses of boys and girls in the class. The boys were heavier. (Comparing two groups)								
We studied how people came to school. The number that came by car was greatest. (Comparing more than two groups)								
Incorrect sentence: Those that went to the fete had the greatest fun. (Should be 'greater' since there are two groups – those that went and those that did not)								
Compare (R) Children compare an enormous number of things in their world – colours, shapes, number of sides, how high they can jump and so on. The trick is to use these opportunities to develop their linguistic skills and understanding of mathematical terms. For example, when comparing heights jumped, do not be satisfied with the fact that one person jumped higher than another, but discuss the heights in centimetres and how much higher one jumped than the other.								
<b>COMPASS POINT</b> A direction on a compass relative to the North direction. There are, of course, two North Poles, the Geographic North Pole and the Magnetic North Pole. The Geographic is the point where the Earth's axis of spin meets the surface of the Earth and does not move over very long periods of time. The Magnetic is currently situated at a point north of Canada and does move at varying speeds over much shorter time scales. A magnetic compass will, of course, point to the Magnetic North Pole, but for us here in the UK the difference in direction between the Magnetic and Geographic North Poles is a very small angle that need not concern children of primary age.								
The compass points children need to know are the eight shown in the diagram below:								



#### Contains (2)

Used to mean 'is held within.'

#### Convex (4)

Used to describe a shape that curves outwards, like the outside surface of a mug or ball. Some mirrors are convex shaped. In this sense it is the opposite of concave.

#### Co-ordinates (4)

A system used to specify a point on a grid. Each point is given two numbers (which may be fractions or decimals). These are distances from a set of axes and are written in round brackets with the horizontal distance first and the vertical distance second. The numbers are separated by a comma.

Each quarter of the grid is called a quadrant and these are numbered starting with the top right quadrant and moving in an anti-clockwise direction.



Point A has co-ordinates (5, 1). Point B has co-ordinates (-5, 4). Point C has co-ordinates (-4, -3). Point D has co-ordinates (2, -2).

These axes have been labelled **x** and **y**, but any suitable letters may be used.

In simpler applications, only the 1st quadrant is used.

#### Corner (R)

A place where two or more edges meet.

### Count (Counting) (R)

- a) The practical process of applying a one-to-one correspondence between the objects being counted and the numbers being used to count. Children need to learn several things before they can count properly:
- (i) The number of objects is always the same regardless of how they may be arranged (conservation of number).
- (ii) The number of objects is always the same regardless of the order in which they are counted.
- (iii) The sequence of numbers 1, 2, 3, 4, 5, etc
- (iv) The fact that the 'number' of objects is the last number used when counting them.
- (v) Each object is counted once and only once.

This is quite a lot to master. Later we ask children to count objects in twos by counting them in pairs (or threes etc).

b) The process of counting in a vacuum, i.e. without any objects. This is done to reinforce their understanding of the number sequence and can sometimes be done using songs (*One, two, three, four, five, once I caught a fish alive...*). We also ask children to count in ones, twos, fives etc without objects to count.

#### Count back from (R)

An introduction to the method of subtraction in which children count back the number to be taken away.

#### Count on from (R)

An introduction to the method of addition in which children count on the number being added.

#### Cube (R)

A three dimensional shape with six square faces. See the major topic THREE DIMENSIONAL SHAPES

#### Cuboid (1)

A three dimensional shape with six rectangular faces. A cube is a special case of a cuboid in which all the edges are equal in length. See the major topic THREE DIMENSIONAL SHAPES

#### Currency (5)

It is important for children to realize that the British pound is only one of many currencies in the world and that the exchange rates vary on a daily basis. Familiarity with the Euro and US Dollar are probably the most important to know for obvious reasons, but it would be good for children to be familiar with currencies from any countries in the world, especially for those from which some members of the class may originate.



Graphs may be drawn showing how one currency converts to another.

#### Cylinder (1)

A three dimensional shape made with circular ends and a curved surface between them.

#### Cylindrical (4)

Shaped like a cylinder. 'The package was cylindrical in shape'.

# Data (4)

Data is the group of individual items collected in a survey or as the result of an experiment etc. Information is what results when this data is organized in some meaningful way, such as finding averages or ranges, or drawing graphs.



**DECIMAL SYSTEM** It is a simple fact that our modern decimal system we use every day is one of the greatest inventions of mankind and it is important for children to appreciate that it is both an invention and great. Without it much of what we know today would not exist. The decimal number system makes it easy to trade, to do engineering calculations, to build computers and to translate sounds into numbers to give us the modern hi-fi digital world in which we live.

To appreciate this fact we need look no further than the Roman number system. The Romans built a large empire and took under their control some of the greatest minds of the time. They gave us roads, house building techniques, aqueducts and a thousand other useful ideas. What they did not give us, however, were any great developments in mathematics and this was largely due to their clumsy number system.

The invention of the modern system changed all that – so what is it about our system that makes it so productive? The answer can be given in just two words – Place Value.



This is the idea that the value of a particular digit is mainly determined by its position in a number and its position can be anywhere from infinity to the left to infinity to the right of the decimal point (although we rarely attempt to push the system to those extreme limits!).

Every operation may be performed anywhere in the number without having to change the rules. **5 + 2** gives **7** no matter whether we are talking about **5** units and **2** units or **5** millions and **2** millions or **5** thousandths and **2** thousandths.

So let us have a look at some important ideas involved in the decimal system.

Firstly, every number has a decimal point which is always placed to the right of the units column. In practice it is not always necessary to include it, but as soon as children are taught about the decimal point, they should also be taught that every number has one.

Secondly, every number floats in a sea of zeroes extending to infinity in both directions even though we don't write all these zeroes in practice. For example, **45.7** can be written as ....**000000000000045.700000000000**....

Teaching children this emphasises to them that the place value columns are still there even though we never use them all and also helps when multiplying by powers of ten. E.g. **36 x 1000 = 36 000**. Where did those zeroes come from? If we think of **36** as ...**00000000036.000000000**.... and we move the digits three places to the left, it is easy to see where the zeroes came from.

All the familiar positions in a number have a name. The names are usually written with an upper case letter to the left of the decimal point and with a lower case letter to the right.

The term 'billion' has caused some confusion over the years because in Britain it meant **1 000 000 000 000** i.e. a million million whilst in the U.S.A. it meant **1 000 000 000** i.e. a thousand million. Today we normally use the American version on both sides of the Atlantic. This has also affected the meaning of the term 'trillion' which is now taken to be the old British billion.

Billions	Hundred	Ten	Millions	Hundred	Ten	Thousands	Hundreds	Tens	Units	tenths h	undredth	s thousandths
3	Millions A	willions 7	2	r nousanos 6	r nousands g	5	٩	Λ	6	5	8	3
•	This displ Three bil hundred	lay show lion, for and for	/s all the u <b>r hund</b> ty six po	e places ch red and se oint five e	ildren will e eventy two ight three.	eventually n million, s	eed to kn ix hundre	ow. T ed an	his nu d eig	umber is hty five	s: thousa	and, nine

Notice that when reading the decimal part, we just give the digits in order. This prevents confusion when two numbers have a different number of decimal digits and we wish to compare them. E.g. **0.83** and **0.237**. If we were to say 'zero point eighty three' and 'zero point two hundred and thirty seven', it would sound as though the second number is larger, which, of course, it is not.

Another great advantage of the decimal system is that to multiply by ten we simply move all the digits to the left one place, two places to multiply by a hundred and so on. To divide, we move one place to the right for division by ten, two places for division by a hundred and so on. When multiplying a whole number by ten the digits move one place to the left and a zero from the right of the decimal point moves left to cross over the point and fill in the gap. In the early stages (before children have come across decimals) all you need to say is that the units column is left empty and so we fill it in with a zero.

Under <u>no</u> circumstances say to your children:

a) 'The decimal point moves to the left or right'. (Since the decimal point is always between the units and tenths columns, how can it move?)

That's right, it never moves!



b) When you multiply by ten 'add a nought'. This causes great contusion later when decimals are multiplied by ten e.g. 3.2 x 10 is not equal to 3.20 !

Never say, 'Add a nought'!



At all times emphasize the movement of the digits to the left or right as appropriate when multiplying by ten, a hundred etc.

#### Decimal (4)

The part of the number which is to the right of the decimal point.

#### Decimal fraction (4)

Another name for 'decimal'. This emphasizes the fact that decimals are really fractions of a whole written in a special way e.g. instead of  ${}^{3}I_{10}$  we write **0.3**.

#### Decimal place (4)

A digit in the decimal part of the number. E.g. the number 45.238 has three decimal places.

#### Decimal point (4)

The 'dot' that separates the whole number part from the decimal part.

#### Decrease (4)

To reduce in size. Can be used for numbers ('Decrease 25 by 10', 'Decrease 40 by 10%') or for shapes ('Decrease this shape in size by 50%).

#### Deep (R)

a) The depth of a liquid or something below the liquid's surface such as a fish.b) The distance from the front of an object (normally a piece of furniture such as a kitchen unit) to the back. E.g. 'kitchen units are now 600 mm deep'.

#### Degree (4)

A small measurement of angle or turn. **360°** make one complete turn, so **90°** make a quarter turn or right angle. Protractors are marked in degrees. Some years ago there was an attempt to introduce a metric degree by which **100** made a right angle. These were called *'grads'* and are still seen on some scientific calculators, but never caught on.

#### **Denominator** (5)

The bottom number in a fraction. The upper number is the numerator. See the major topic FRACTIONS.

#### Depart (4)

To leave. Used mainly in timetables.

#### Depth (R)

The noun of 'deep'.

#### Descend (3)

To go down as in descending a snake in the game of snakes and ladders.



#### Diagonal (3)

A line drawn from one corner to another of a two dimensional shape or from one vertex to another of a three dimensional shape.

# Diameter (4)

The distance or the line from one side of a circle to the other, passing through the centre.

#### Die, dice (R)

Strictly speaking, 'dice' is the plural of the word 'die', a cube showing six numbers, one on each face, but not many people seem to know that, so over the years the word 'dice' has been taken to mean a single die as well as many dice. As only mathematics teachers seem to be concerned about this, there seems little chance of reverting to the correct usage of these words.

Dice are also used in games such as snakes and ladders and children should play these games often because, not only do they give practice in counting, they also give a feel for the generation of random numbers which will be useful later in life when they study probability.

Of course, any six numbers may be placed on a dice and it is possible to obtain dice with even numbers. positive and negative numbers etc for use in mathematics lessons. Despite this, the vast majority of dice are produced with the numbers 1 to 6, but these are not placed randomly. The rule that is in common use is that the numbers on opposite faces of a dice add up to 7. Surprisingly, there are only two ways of doing this and we can see the difference if we look at one corner of the dice:



In the left dice the numbers increase from 1 to 3 in an anti-clockwise direction. This is known as a left handed dice. In the right dice they increase in a clockwise direction. This is known as a right handed dice. Any dice that obeys the rule that opposite faces add up to 7 may be held in this way to see if it is a left handed or right handed dice. Most commercially produced dice are left handed.

# MathSphere dictionary for teaching assistants Difference between (R) How many you need to add one number to arrive at another. E.g. the difference between 5 and 18 is 13. When children first encounter the concept of 'counting on', they want to count the starting number as the first and get an answer which is one too big. They need to be taught that the first number is the starting position and the first number to be counted is the next number. E.g. 'What is the difference between 4 and 8 ?' 4 5 6 7 8 Starting point First number to be counted Digit (1) One of the number 0 to 9 as in 'The number 462 has three digits', 'The fifth digit in 84.38742 is 7' and, in secondary mathematics, 'The most significant digit in 63.82 is 6'. Digital/analogue clock/watch (2) As far as young children are concerned, the difference between a digital and an analogue clock or watch is simply that a digital clock has only numbers and an analogue clock has hands that rotate over a numbered scale (normally 1 – 12, but not always). (See 'Clock' for illustration). If, however, you are interested in a more technical definition, please read on. The word analogue is used to describe an object or system which imitates in some way a completely different concept. For instance, the older type of voltmeter with a moving needle shows the voltage connected to it and can move left or right over a numbered scale as the voltage changes. The reading on the scale is not the voltage, but it imitates it in a rather clever way so that we can 'see' the level of voltage being applied. Similarly, the mercury in a thermometer moves up and down as the temperature rises and falls. Again the height of the mercury is not the temperature, but imitates its value and variation. We say the movement of the voltmeter needle is an 'analogue' of the voltage changes and the level of the mercury is an 'analogue' of the temperature changes. The same applies to a clock, that is the type with a nice round face and moving hands. As the time passes, the hands move around in a corresponding way and enables us to measure the passing of time and say what time of day it is. The snag is that the passing of time is a continuous and smooth happening and so the movement of the hands must be equally smooth. Some clocks do have smoothly moving hands and so are pretty close to proper analogue devices, but some have second hands that 'click' over every second or even minute hands that 'click' over every minute. Strictly speaking, therefore, these are not analogue clocks, but digital - a word used to describe a system in which the measurements are divided into discrete steps with nothing in-between. But we do not recommend that you try to explain this subtle difference to seven year olds. Life's a funny thing! Direction (R) Directions allow a route to be shown in several ways: left, right, up, down etc and the points of a compass. Giving directions to go to the shops or from school to home is good practice. See the major topic COMPASS DIRECTION. Discount (5) An amount that has been deducted from the original price of an object. It may be given in several ways: the discount in money ('£5.00 discount'), in percentages ('30% discount') or as a fraction ('one quarter off!'). Often today we see bargains such as 'three for the price of two' which are discounts in disguise. Display (5) The part of a calculator in which the questions and answers are displayed as we type them in.

Distance apart, between, to, none (5)
In simple cases, distance between two objects is normally given as the shortest distance (as the crow
flies). When this is not the case (such as the distance between towns along existing roads) this fact
should be stated if it is not already clear from the context. (London to Brighton is <b>100 Km</b> along the A23
and M23 etc).
Distribution (6)
The way data is spread over a range of values. E.g. The number of people that obtained between
1 and 10 marks, 11 and 20 marks, 21 and 30 marks etc in a test'.
The idea that one number will divide exactly into another. There are some divisibility tests with which
children should be familier
A number is divisible by <b>2</b> if the last digit is divisible by <b>2</b> (even)
A number is divisible by $4$ if the last two digits are divisible by $4$
A number is divisible by 8 if the last three digits are divisible by 8 etc.
A number is divisible by 3 if the sum of the digits is divisible by 3 E a. 276 is divisible by 3 because
A number is divisible by 5 if the sum of the digits is divisible by 5. E.g. 276 is divisible by 5 because $2 \pm 7 \pm 6 = 16$ and 15 is divisible by 3
$2 \cdot 7 \cdot 6 = 10$ and 10 is divisible by <b>3</b> .
A number is divisible by 5 if the last digit is $0 \text{ or } 5$
A number is divisible by <b>10</b> if the last digit is <b>0</b>
A number is divisible by $100$ if the last two digits are $00$ etc.
Some combinations are possible such as:
A number is divisible by <b>6</b> if the last digit is even and the sum of the digits is divisible by <b>3</b> .
, , , , , , , , , , , , , , , , , , , ,
Divisible by (4)
The fact that one integer will divide exactly into another integer with no remainder.
Division (3)
Did you know there are two aspects to division, the
'sharing' and the 'how many times' ideas?
With the 'sharing' idea, we take a number of objects and share them between a number of people and see
With the ' <i>sharing</i> ' idea, we take a number of objects and share them between a number of people and see how many they receive each. E.g. divide <b>12</b> by <b>4</b> is seen as sharing twelve objects between four people.
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#### Dominoes (R) Great game to encourage counting and matching. Children should play a lot more of these games. When children are young, the traditional type of dominoes should be used, but later you can make up your own to match, for example, multiplication sums with the answers. On one square you write 3 X 4 and on another square on a different domino, you write 12 or 2 x 6. It is not difficult to build a complete set of dominoes which can be used to play according to the usual rules.

Other options include equivalent fractions, fraction sums such '2 x 3/4', percentages to fractions etc.

But dominoes have another use altogether. The arrangement of dots provides a good opportunity for investigation. In most parts of the UK people play with dominoes with a maximum of six spots, but in some parts of the country people play with dominoes with a maximum of nine spots. There are **28** dominoes in the first set and **45** in the second. Both of these are triangle numbers. Would that always be the case, regardless of what the maximum number of spots was or is it just a coincidence?



#### Eighth (4)

a) See the major topic CARDINAL and ORDINAL NUMBERS.

b) One eighth as a fraction:  $1/_8$ . One whole divided by eight.

#### Eleven (1)

See the major topic CARDINAL and ORDINAL NUMBERS.

#### Eleventh (1)

a) See the major topic CARDINAL and ORDINAL NUMBERS.

b) One eleventh as a fraction:  ${}^{1}I_{11}$ . One whole divided by eleven.

# Enter key (5)

The key on a calculator or computer keyboard that signals the end of an entry.

#### Equal chance (6)

When things have the same probability of happening. E.g. 'There is an equal chance of obtaining a head or a tail when a coin is tossed', 'There is an equal chance of obtaining any of the numbers on a normal dice when it is thrown'.

#### Equal groups of (2)

An introduction to the idea of division by dividing a number of objects into equal sized groups.

#### Equal parts (2)

Parts of the same size.

#### Equal to (1)

When one part is the same size as the other. This may be as simple as  $2 \times 3$  equals 6 or more complicated such as equivalent fractions:  ${}^{4}I_{5} = {}^{36}I_{45}$ 

#### Equally likely (6)

When things have the same probability of happening. E.g. 'There is an equal chance of obtaining a head or a tail when a coin is tossed', 'There is an equal chance of obtaining any of the numbers on a normal dice when it is thrown'.

#### Equals (1)

See 'Equal to'.

#### Equals sign (=) (1)

The sign used to indicate equality.

#### Equation (3)

A mathematical sentence in which symbols on the left and symbols on the right are separated by an equals sign. Sometimes it is written to indicate a sum and an answer such as  $5 \times 4 = 20$  and sometimes to indicate a relationship with an unknown that needs to be found, a process called 'solving the equation', such as 2x + 5 = 17.

#### Equilateral triangle (4)

A triangle with three equal sides and three equal angles. See the major topic TWO DIMENSIONAL SHAPES

#### Equivalent (5)

Equivalent fractions are fractions that look different but have the same value such as  $\frac{1}{2}$  and  $\frac{2}{4}$ . See the major topic FRACTIONS.

#### Estimate (R)

A guess based on experience.

MathSphere dictionary for teaching assistants
Even (R) One of the numbers8, -6, -4, -2, 0, 2, 4, 6, 8,, although in the early stages children will only handle positive even numbers and zero.
Even chance (6) See 'Equal chance'.
<b>Every other</b> (R) The process of taking one and missing one repeatedly. E.g. 'Starting at <b>1</b> , every other number is odd'.
Exactly (2) An indication that there is no error in a calculation or measurement. E.g. 'The number of people in the crowd was exactly 387.'
<ul> <li>Exchange (1)</li> <li>a) Used for the process of swapping one in the tens column for ten units.</li> <li>b) Used when swapping money in one currency for money in another.</li> </ul>
Face (R) One of the surfaces of a three dimensional shape.
Factor (4) A number that will divide exactly into another. E.g. 'The factors of 12 are 1, 2, 3, 4, 6, and 12.'
Factorise (6) The process of finding the factors of a number.
<ul> <li>Fair (5)</li> <li>a) An experiment in which the outcomes are fairly generated, for example when you throw a fair dice or spin a fair spinner.</li> <li>b) A fair survey is one in which the data is not biased towards one group or particular idea.</li> </ul>
Fast (1) Quick; covers a large distance in a short time.
Faster (1) See the major topic COMPARATIVE and SUPERLATIVE.
Fastest (1) See the major topic COMPARATIVE and SUPERLATIVE.
February (2) See the major topic TIME.
Feet (6) Plural of 'foot'.
<ul> <li>Fifth (4)</li> <li>a) See the major topic CARDINAL and ORDINAL NUMBERS.</li> <li>b) One fifth as a fraction: <sup>1</sup>/<sub>5</sub>. One whole divided by five.</li> </ul>
<b>Fifty-fifty chance (6)</b> Describes an event in which there are two possible outcomes, both of which have a <b>50%</b> chance of happening.
Figures (2)

Another word for 'digits'.

First, second, third etc (R) See the major topic on CARDINAL and ORDINAL NUMBERS.

**Fold (2)** Often used when demonstrating that a shape has symmetrical symmetry or when making three dimensional shapes.

#### Foot (6)

An imperial measure equal to 30.48 cm. See the major topic IMPERIAL UNITS.

#### For every (4)

Used when describing patterns. E.g. 'For every square there are four circles'.

#### Formula (5)

Any expression that describes how to find the answer to a particular problem. Initially written in words: 'To find the fifth square number, multiply five by itself.' And later in symbols: 'The area **A** of a rectangle is given by the length **I** multiplied by the width **w**. In other words  $\mathbf{A} = \mathbf{Iw}$ .'





I.e. C = 
$$\frac{\sqrt{((hm)^2 + N)}}{D}$$

Alternatively, a very large piece will do nicely, thank you very much!

#### Fortnight (2)

A period of two weeks. On its own it normally starts on a Sunday and finishes on a Saturday, but can be from any day of the week depending on the context.

#### Four digit number (4)

A number with four digits, normally thousands, hundreds, tens and units.

#### Fourth (R)

See the major topic CARDINAL and ORDINAL NUMBERS.

#### FRACTIONS

Many people believe that now we use mainly a decimal system in everyday life, it is no longer necessary to teach fractions. Nothing could be further from the truth. We often come across fractions in everyday life (in sale price reductions, for example); there is a close relationship between percentages, decimals and fractions of which children should be aware and fractions are still used a great deal for interest rates. In addition to this, however, there is a more subtle use. As we shall soon see, a fraction may be regarded as a division sum and fractions are therefore an easy way to give an answer to a division problem when it is not an easy matter or is indeed completely impossible to give a numeric answer. The most obvious example of this is when dealing with algebra.

The manipulation of fractions involves many concepts and the teaching of these should not be rushed. Teachers have spent many years trying to teach the manipulation of fractions (by which we mean addition, subtraction, multiplication and division) by what has been, to all intents and purposes, a series of tricks. We are pleased to see that the Numeracy Strategy Document has at last recognized this fact and has recommended that before year seven, children confine their learning to understanding the nature of fractions, finding fractions of given amounts (e.g.  $\frac{2}{3}$  of **600**) and similar ideas.

Under this topic heading we shall be going a little further into the processes involved and delving into work of higher year groups to illustrate how important the work of the lower year groups is in developing an understanding of the processes that will be required in later mathematical life.



This is more useful because it enables us to answer questions of three different types:

- **Type 1**: E.g. What is **7** divided by **16** ? Why, <sup>7</sup>*I*<sub>16</sub>, of course. We see from this it is not always necessary to give an answer as a decimal.
  - E.g. What is  $\mathbf{a} \div \mathbf{b}$ ? Answer  $a_{l_b}$ .
- **Type 2**: E.g. Write  ${}^{7}I_{15}$  as a decimal. As we know a fraction is a divide sum, we simply divide **7** by **15** on our calculator.

**Type 3**: E.g. Find  $\frac{3}{4}$  of **£6.40**. To answer this we realize that finding  $\frac{3}{4}$  of a quantity means finding one quarter of it by dividing by **4** and then multiplying by **3**. **£6.40** ÷ **4** = **£1.60**. **£1.60** x **3** = **£4.80**.

Terminology: The upper number in a fraction is called the 'numerator' and the lower number is the 'denominator'.

Equivalent fractions. Equivalent fractions are the single most important concept to understand when learning about fractions and no real progress can be made until they are thoroughly mastered. It is certainly possible to teach children the tricks mentioned earlier, but tricks are soon forgotten unless regularly practised and understanding will be lacking.

Firstly, what are equivalent fractions? Two or more fractions are said to be equivalent if they have the same value, even though they look different. E.g.  ${}^{2}/_{3}$ ,  ${}^{4}/_{6}$ ,  ${}^{300}/_{450}$  and  ${}^{4000}/_{6000}$  are all equivalent because they are equal to  ${}^{2}/_{3}$ .

It is possible to change a fraction into an equivalent fraction in two ways:

The first is called <u>cancelling</u> and is carried out by dividing both the numerator and the denominator by the same number. E.g.  ${}^{24}I_{30}$  become  ${}^{4}I_{5}$  by dividing both **24** and **30** by **6**.

The second is called <u>lecnacing</u> and is carried out by multiplying the numerator and the denominator by the same number. E.g.  ${}^{3}I_{7}$  becomes  ${}^{12}I_{28}$  by multiplying both **3** and **7** by **4**.

Thus a series of equivalent fractions may easily be constructed. For example, begin with the fraction  ${}^{3}I_{5}$  and lecnac by **2**, **3**, **4** etc in turn:

 ${}^{3}I_{5}, {}^{6}I_{10}, {}^{9}I_{15}, {}^{12}I_{20}, \dots {}^{60}I_{100}, \dots {}^{300}I_{500}$  etc

It can easily be seen that the sequence could have been constructed by starting on the right and cancelling.

An interesting teaching point is to get the children to think of fractions as spies. The fraction in its lowest terms (i.e. fully cancelled) is the 'naked' spy whose identity is easily determined. As the fraction is lecnaced by higher and higher numbers, he/she acquires more and more disguise until he is almost unrecognizable. Although his identity is now more difficult to determine, he is still the same fraction underneath!

To fully appreciate the importance of equivalent fractions let us look at some examples.

E.g. Calculate  ${}^{3}/_{5} + {}^{5}/_{6}$ .

 ${}^{3}/_{5} + {}^{5}/_{6} = {}^{18}/_{30} + {}^{25}/_{30} = {}^{43}/_{30} = \mathbf{1}^{13}/_{30}$ 

First we find a number that the two denominators (**5** and **6**) will divide into. This is obviously **30**. Next we lecnac  ${}^{3}I_{5}$  by **6** to obtain  ${}^{18}I_{30}$  (equivalent fractions) and  ${}^{5}I_{6}$  by **5** to obtain  ${}^{25}I_{30}$  (equivalent fractions). We add to make  ${}^{43}I_{30}$ .

At this point we realize we have an improper fraction (one in which the numerator is greater than the denominator) so we take  ${}^{30}I_{30}$  (=  ${}^{1}I_1$  = 1 equivalent fraction) from  ${}^{43}I_{30}$  giving the mixed number  $1{}^{13}I_{30}$ . We have used equivalent fractions three times in this simple calculation. Sometimes the fraction part of the mixed number will cancel forcing us to use equivalent fractions again.

# E.g. Calculate <sup>3</sup>/<sub>5</sub> x <sup>15</sup>/<sub>20</sub>.

Multiply the numerators together and the denominators together to obtain  ${}^{45}/_{60}$ . Cancel by **15** to get  ${}^{3}/_{4}$ . Again we have used equivalent fractions.

This obvious method can easily produce very large numbers in the numerator and denominator so in practice we normally do some cancelling before multiplying. This need not concern us here except to say that this involves an even greater use of equivalent fractions.

E.g. Write  $3^4/_{15}$  as an improper fraction.

Recognize that **3** is  ${}^{3}I_{1}$  and this may be lecnaced to  ${}^{45}I_{15}$  (equivalent fractions). Then add the  ${}^{4}I_{15}$  to obtain  ${}^{49}I_{15}$ .

In fact, almost every operation involving fractions also involves equivalent fractions, so it is very important to make sure that children really understand the concept and how to change any given fraction into a set of equivalent fractions.

# Frequency table (3)

A table that shows the frequency with which things occur. E.g. 'This is a frequency table of the number of deliveries made by a lorry driver each day in one week:

Monday23Tuesday18Wednesday18Thursday26Friday21Saturday12

#### Friday (2)

See the major topic TIME.

#### Further (2)

See major topic COMPARATIVE and SUPERLATIVE.

#### Furthest (2)

See major topic COMPARATIVE and SUPERLATIVE.

#### Gallon (5)

See the major topic on IMPERIAL UNITS.

#### Geo strips (2)

Flexible rods providing a visual means for children to investigate the relationships between geometric shapes. Using them, they can explore the angles, area, and perimeters of shapes.

# Good chance (5)

Having a high probability.

### Gram (2)

One thousandth of a kilogram. See the major topic METRIC SYSTEM for more details.





#### Heptagon (4)

A polygon with seven sides. See the major topic TWO DIMENSIONAL SHAPES

#### Hexagon (2)

A polygon with six sides. See the major topic TWO DIMENSIONAL SHAPES

#### Hexagonal (3)

In the shape of a hexagon.

#### High (R)

See 'Height'.

#### Higher (2)

When one object is taller than another or placed at a higher point relative to sea level.

#### Highest (R)

The tallest object or the object placed at the greatest height above sea level.

#### Holds (R)

The capacity of a container.

## Horizontal (3)

Parallel to the Earth's surface locally.

#### Hour (R)

See the major topic TIME.

#### Hundred square (2)

There are two versions of this:

a) A square of ten rows and ten columns on which the numbers **1** to **100** written, normally starting at the top and working from left to right.

b) The same, but starting at **0** and finishing at **99**.

Each type has its advantages.

#### Hundred thousand (4)

See the major topic on the DECIMAL SYSTEM.

#### Hundreds (2)

See the major topic on the DECIMAL SYSTEM.

#### Hundreds boundary (3)

Used to discuss what happens when adding or subtracting a number to another number takes us into the next hundred. E.g. Adding **23** to **488** involves crossing the **500** boundary.

#### Identical (6)

When two things are exactly the same. This could be two- or three-dimensional shapes or the average height of boys and the average height of girls in a class etc.
#### **IMPERIAL UNITS** A system of units that should have felt the kiss of death years ago, but refuses to go away despite the fact it is no longer taught as the main system of units in schools today. There are some imperial units still in use and these are given below with their approximate metric equivalents: Mile 1.6 kilometres Pint Just over half a litre About 4.5 litres Gallon Yard Just less than a metre Foot About 30 cm Inch About 2.5 cm Pound Just less than half a kilogram Ounce About b grams Here they are in reverse: Kilometre 0.6 miles 1.75 pints Litre Litre 0.2 gallons Metre Just over a yard Just under half an inch Cm Kilogram About 2.2 pounds Gram About one thirtieth of an ounce Impossible (5) When teaching probability it is important to recognize that some events are actually impossible. Children often have difficulty understanding the difference between impossible and very unlikely. Many unlikely events such as the Sun not rising tomorrow, a bridge being built over the Atlantic Ocean and men giving birth (you never know with the miracles of modern medicine), are seen by children as impossible. Because of this it is often a good idea to stick to simple 'impossible' events such as throwing a seven with a normal 1 - 6 dice. Impossible events have a probability of zero whilst unlikely events have a probability slightly higher than zero. Improper fraction (5) A ridiculous name for a fraction in which the numerator is greater than the denominator (as if it were improperly dressed in some way!). In every (4) Used in work on fractions. If one in every four girls enjoys roller blading, this can be translated into 'one quarter of girls enjoy roller blading'. Similarly with probability: If one in every six cars coming off a production line has a fault, then the probability of any particular car having a fault is one in six or one sixth. Inch (6) A member of the system of units known as the Imperial system. An inch is 2.54 cm long. See major topic IMPERIAL UNITS. Increase (4) To make larger. Can be used for numbers ('Increase 25 by 10', 'Increase 40 by 10%') or for shapes ('Increase this shape in size by 50%).

# INTEGERS

Integers are whole numbers and may be negative, zero or positive. Examples of integers are **100**, **1**, **0**, **3**, **350**. The name 'minus' is often used to describe negative numbers especially when referring to temperature, although this can be confusing (See <u>minus</u>).

Positive numbers are thought of as being 'above' zero, negative numbers 'below' zero and zero itself as a sort of neutral fence sitting between them.

Teaching children to use operations with negative numbers can be quite challenging, but it is quite usual to expect older primary children to be able to carry out some simple operations so they may begin to understand the processes. As far as possible examples should be taken from the real world:

E.g. The temperature is <sup>-5°</sup>C. What will the temperature be if it rises 12°C?

E.g. I have **£15.00** in the bank. If I write a cheque for **£20.00**, how much money will I have in the bank (assuming the bank agrees to process the cheque, of course)?

The second example would result in a new balance of **£5**, but we normally refer to this as **£5** overdrawn or 'in the red' and it should be pointed out to children that sometimes mathematical language differs from 'real world' language.

[As a historical note, the reason the phrases 'in the red' and 'in the black' are used is that before computers were used by banks, the typewriters they used had ribbons with two colours, black and red. The positive balances were typed in black and the overdrawn balances were typed in red.]

Number lines with integers can also be used to indicate position. Two such axes are drawn at right angles (see <u>co-ordinates</u>) and points may be plotted by referring to a pair of co-ordinates. Later, of course, the spaces between the integers are filled in with decimal numbers so that many more points may be plotted.

# International Date Line (6)

An imaginary line approximately opposite the Greenwich Meridian ( $\mathbf{0}^{\circ}$  longitude) which separates one day from another.

Imagine it is **6 p.m**. on Wednesday in London. As we move east the hour of the day increases every time we pass through a time zone. **7 pm.**, **8 p.m**. and so on until we get to midnight on Wednesday evening. By this time we will be one quarter of the way around the world. We continue: **1 a.m.**, **2 a.m.** ... **6 a.m.** Now we are half way around the world – but what day is it? Pretty obviously it is now Thursday. Go back to London at **6 p.m.** on Wednesday. This time go west: **5 p.m.**, **4 p.m.**, .... By the time it is 6 a.m. we will be half way around the world again, but this time it is still Wednesday!

Wednesday meets Thursday on the opposite side of the world to London. The line at which this happens is known as the International Date Line. Any good atlas shows it clearly. It is not a straight line going from the North Pole to the South Pole. It wiggles a little to bypass islands and countries, otherwise some islands would have one day on their eastern sides and a different day on their western sides, even though it would be the same time of day.

# Intersecting (6)

Two lines that cross each other are called *'intersecting*'. This idea occurs in the intersection of axes on a graph, diagonals of polygons as in *'The diagonals of a rhombus intersect at right angles,'* and in some interesting situations to investigate such as the number of points of intersection from two given points in a straight line to any number of other points in a parallel straight line:







3 Intersections

6 Intersections

10 Intersections

#### Inverse (4)

Opposite. Used initially to name the idea that subtraction is the opposite of addition and division is the opposite of multiplication etc, but is later extended to such things as square rooting is the opposite of squaring and the solving of algebraic equations.

#### Irregular (4)

Normally used to refer to a polygon that does not have all its sides the same length and all its angles equal or a polyhedron whose faces are not all regular polygons.

#### Isosceles triangle (4)

A triangle with two equal sides and two equal angles. See the major topic TWO DIMENSIONAL SHAPES.

# January (2)

See the major topic TIME.

#### Journey (1)

Travelling from one place to another. Used in mathematics to reinforce the idea of position (perhaps by the use of co-ordinates) and directions (left, right, north, south etc).

#### July (2)

See the major topic TIME.

# June (2)

See the major topic TIME.

#### Key (5)

- a) A calculator key
- b) A key on a map showing the scale of the map.

#### Kilogram (2)

The fundamental measure of mass in the metric system. See the major topic METRIC SYSTEM for more details.

# Kilometre (3)

One thousand metres. See the major topic METRIC SYSTEM for more details.

#### Kite (6)

A quadrilateral with two pairs of adjacent equal sides. See the major topic TWO DIMENSIONAL SHAPES.

#### Label (2)

Refers to the label given to the axes on a graph. Every graph should have a title and its axes labelled.

#### Larger (R)

See the major topic COMPARATIVE and SUPERLATIVE.

# Largest (R)

See the major topic COMPARATIVE and SUPERLATIVE.

# Last but one (R)

Penultimate.

# Layer (3)

Used in calculating volume as in '*The volume of one layer of the cuboid is* **60** cm<sup>3</sup>'.

#### Leap year (4)

A year which has **366** days, the extra one being provided by **February 29<sup>th</sup>**. See the major topic TIME.

# Least (R)

Smallest number or amount.

# Least common (2)

The number or object that occurs fewest times.

#### Least popular (2)

The item that is chosen by the smallest number of people.

#### Least value (3)

The item that gives the worst deal for the customer.

#### Lecnac (5)

The operation of changing a fraction into a more complex equivalent fraction by multiplying the numerator and denominator by the same number. See the major topic FRACTIONS.

#### Length (R)

The distance from one end of an object to the far end.

#### Less than < (4)

This sign means 'less than' and for a true statement to be made, the value on the left must be less than (not equal to) the value on the right.

#### 30 ÷ 5 <4 x 6.5, E.q. 3 < 5, are correct uses.

E.g. 2 x 15 < 6 x 5 is an incorrect use.

As an aide memoir, both the 'greater than' sign (>) and the 'less than' sign ('<') always point to the smaller value.

#### Less than or equal to $(\leq)$ (5)

As above, but includes 'equal to'. In this case  $2 \times 15 \le 6 \times 5$  is true.

#### Less/least expensive (3) Cheaper/cheapest.

# Light (R)

As in the sense of 'not heavy'.

#### Lighter (R)

See major topic COMPARATIVE and SUPERLATIVE.

## Lightest (R)

See major topic COMPARATIVE and SUPERLATIVE.

#### Likelihood (5)

A word used to express the probability of something happening. E.g. 'The likelihood of Rain in Birmingham tomorrow is about 20%.

# Likely (5)

A word used to indicate that something has a probability of happening greater than 50%, i.e. there is more probability of it happening than not happening.

#### Line graph (5)

A graph in which plotted points are joined with a line. The points between the plotted points must be meaningful. E.g. points in a graph of temperatures in a living room plotted every ten minutes can normally be joined because the points between do exist in real time and each has a corresponding temperature.

On the other hand, twelve points plotted on a graph to represent total sales in each month of a given year should not be joined because the points between are meaningless (what does a point between June and July mean, for example. Despite this, people often do join them up.

MathSphere dictionary for teaching assistants
Line of symmetry (2) A line passing through the middle of a shape with reflective symmetry so that the half on one side is a reflection of the other half in the line. Often called the <i>'mirror line'</i> or <i>'axis of symmetry'</i> .
Line of Symmetry or Axis of Symmetry or Mirror Line
Line symmetry (4) If a shape has reflective symmetry, i.e. one half of the shape is a reflection of the other half, it is said to have 'line symmetry', the line referring to the mirror line through the middle (See 'Line of Symmetry' above).
Litre (2) The volume of a cube <b>10 cm x 10 cm x 10 cm</b> . See the major topic METRIC SYSTEM for more details.
Long (R) A relative term like <i>'heavy'</i> . An object can be long compared to a smaller object but not at all long compared to a much bigger one.
Longer (R) See the major topic COMPARATIVE and SUPERLATIVE.
Longest (R) See the major topic COMPARATIVE and SUPERLATIVE.
Loss (6) This can be given as an amount of money, <i>'Harry bought a car for £500 and sold it for £450. He made £50</i> <i>loss'</i> , or as a percentage of the <u>original</u> price. In the example given, Harry made £50 loss on an original price of £500, i.e. 10%.
As a teaching point, profit and loss are almost always calculated as a percentage or fraction of the <u>original</u> price.
Lots of (2)
Working in groups of objects introduces the concept of multiplication: 'Three groups of four are twelve.'

# Lower (2)

See the major topic COMPARATIVE and SUPERLATIVE.

# Map (3)

A representation on paper drawn to scale of an area of land. Used as an introduction to scales and the idea that a short distance on a map can represent a much longer distance in real life. May also be used to reinforce co-ordinates as these may be drawn over a map and used for treasure maps, for example.

# March (2)

See the major topic TIME.

# MASS and WEIGHT

There is a great deal of confusion between the terms mass and weight. The term mass is normally used correctly but the term weight is often used to mean mass as well as weight.

Mass is the amount of substance in an object and is measured in grams, kilograms or tonnes. Provided nothing is taken from or added to an object, its mass will remain constant no matter where in the universe it is taken. The gravity on the Moon, for instance, is about one-sixth that on Earth, but an object with a mass of **6 Kg** on the Earth will still have a mass of **6 Kg** on the Moon because the amount of matter it contains has not changed.

Weight, on the other hand, is the force by which an object is pulled towards the centre of a planet or moon it happens to be sitting on. This is measured in newtons. Here on Earth, a **1 kg** mass is pulled down with a force of approximately ten newtons, a **2 Kg** mass with a force of approximately twenty newtons and so on. On the Moon, however, the weight of objects is about one sixth that on Earth because the Moon's gravity is weaker. A child with a mass of **36 Kg** will therefore weigh about **360** newtons on Earth, but only **60** newtons on the Moon.

Two stories illustrate this difference quite well:

Nellie the elephant was invited to the ball, but when she came to try on her party dress she discovered she had been eating too many cream cakes and the dress, of course, would not fit. She had heard that astronauts are weightless in space so she hitched a ride on the Space Shuttle but found to her horror that although she no longer had any weight, she still had plenty of mass!

A boy was asked in an examination, 'What is the difference between mass and weight?'. He wrote, 'Mass is when you buy a sack of potatoes. Weight is when you have to carry them home.'

The above describes the technical situation and formal definitions. In practice, however, the situation is quite confused. People ask how much you weigh when they should be asking what your mass is. This starts at a very young age and is well ingrained before children are old enough to understand the difference. The problem is compounded by the fact that we measure the mass of an object by weighing it! This is a very convenient way to find the mass of an object, but is by no means the only method. How do astronauts weigh objects and chemicals in space when they are in a weightless environment? One method they use is to put the object whose mass is required into a small box which is fixed to a steel wire that is tensioned rather like a guitar string. The box and string are set vibrating. A more massive object in the box will vibrate more slowly than a less massive one. A computer then measures the number of vibrations per second and from this it is able to calculate the mass of the object. No gravity required!

It would be wonderful if we could teach children the difference between mass and weight from the beginning of their school education, but there are two difficulties that prevent this. Children first need to understand the 'conservation of mass' - the mass of an object remains the same provided you do not add anything or take anything away. A piece of clay can be constantly reshaped, but it always has the same mass. This is obvious to adults, but is, in fact, a concept that needs to be discovered by play and experiment. Secondly, children do not have an understanding of 'force' and the fact that it is the Earth's gravity that stops us floating away and gives us 'weight'. In fact, many adults think it is the atmosphere that stops us floating away and hold us to the Earth's surface. Until children have understood the concept of the conservation of mass and that it is the Earth's gravity that gives us weight, it is impossible for them to appreciate the difference between mass and weight.

For further discussion about the units used for mass and weight, see the major topic 'Metric System'.

# Match (R)

The result of comparing different patterns and noticing that two are the same.

# Maximum (5)

The highest value of a variable. E.g. 'The maximum temperature today will be  $23^{\circ}$ C.' 'What is the maximum amount of liquid this glass can hold?'

# May (2)

See the major topic TIME.

# Mean (6)

There are three types of average – mean, median and mode. The mean is the answer when all the numbers are added together and the total is divided by the number of items.

E.g. The mean of 5, 8, 3, 12, 6 is (5 + 8 + 3 + 12 + 6) ÷ 5 = 34 ÷ 5 = 6.8

The term 'average' is used in everyday language to indicate 'mean' unless it is clear that the median or mode is required.



# Measure (R)

The process of measuring is more complicated than most people imagine. To measure properly you need a unit with which to measure and a starting point. Children often see the need for the unit, but do not appreciate the need for a starting point. This is true whether they are using a ruler, protractor, weighing scale or measuring cylinder. If you watch children using a ruler (especially the type with an extra bit of wood or plastic at the end to protect the scale) they often begin at the end of the ruler, not at the first mark. When using a protractor they often make the same mistake and when using a weighing scale they forget to set it to zero before they put anything in the pan. It is important to establish the proper principles of measuring before asking them to measure to the nearest millimetre, gram etc.

Once they have learnt these principles, the next thing to concentrate on is accuracy of measurement. Children are too often happy with any result, whether it approximates to the true measurement or not. They must therefore be taught that accuracy and careful measurement are essential. This all comes with practice, but too often not enough practice is given.

#### Measurement (4)

The answer to the measuring process!

# Measuring cylinder (4)

A cylinder with markings up the side, normally in millilitres, used to measure the volume of liquids.



# Measuring scale (2) Every measuring instrument needs a measuring scale, whether it is a ruler, measuring cylinder or weighing scale. In other words, the instrument needs to be 'calibrated'. It is important that children are given a lot of practice with traditional measuring instruments with scales before being allowed to use modern digital types with an electronic scale. There are two problems with these: the first is that there is no scale to see - children can easily get the impression that the measurements are produced by 'magic'. After all, many of them still believe in Father Christmas and the Tooth Fairy! The other is that because they are digital, children think they are extremely accurate in their readings. While they do tend to be guite accurate, they do vary in their readings slightly and this can be pointed out to children by using two or more electronic devices to make the same measurement. And don't let them forget: electronic digital devices need to be properly zeroed just like non-digital devices! Median (6) Given a set of numbers, the median is the middle number when all the numbers are placed in numerical order. If there are an even number of numbers in the set, the median is the mean of the two middle ones when placed in order. E.g. Set of numbers: 4, 3, 7, 2, 8 Put in order: 2, 3, 4, 7, 8 The median is therefore 4 E.g. Set of numbers: 18, 25, 34, 15, 25, 19 Put in order: 15, 18, 19, 25, 25, 34 The median is therefore the mean of 19 and 25, i.e. (19 + 25)/2 = 22. Memory (6) A place in a calculator where a number may be stored while another part of a calculation takes place. There are keys for moving a number from the display to the memory and from the memory to the display as well as adding and subtracting the content of the memory directly. Mental calculation (2) A calculation done in one's head. It is normally regarded as permissible to jot down essential numbers or facts on paper as long as the calculation is performed mentally. Method (3) A way of achieving an end result. For example, there are several methods of adding two two-digit numbers together. Metre (1) The fundamental measure of length in the metric system. See the major topic METRIC SYSTEM for more details. Metre stick (1) A piece of wood or plastic that is one metre long. It is often subdivided into centimetres or centimetres and millimetres. Metric unit (4) One of the units such as metres and grams that are used in the metric system. See the major topic METRIC SYSTEM.

# METRIC SYSTEM

The system of units used in most countries of the world (with one or two notable exceptions such as the U.S.A., but even here the metric system is used for most scientific calculations).

A system of units is defined from three fundamental units: time, length and mass. In the metric system the units that correspond to these are second, metre and kilogram respectively. (There are others to define electrical units etc, but these need not concern us here.)

Time: At primary school level, time is always measured in seconds in the metric system. (Minutes, hours, days etc, whilst very useful units in everyday life, are strictly speaking outside the metric system)

Length: The basic unit is the metre. This is divided into millimetres and multiplied up to kilometers. **1000 mm = 1 m** As the millimetre is quite a small unit for children, we also use the centimetre. **100 cm = 1 m 10 mm = 1 cm** 

Area: It follows from the above that the basic unit of area must be the square metre (the area of a square  $1m \times 1m$ ). This is normally written ' $m^{2}$ ', but as this is a difficult concept for young children, it is often useful to allow them to write 'sq.m' instead, changing them over to ' $m^{2}$ ' when you feel they are ready. Similarly a square millimetre, square centimetre and square kilometre may be written as 'sq mm', 'sq cm' and 'sq km' until children are ready for 'mm<sup>2</sup>', 'cm<sup>2</sup>', and 'km<sup>2</sup>' respectively. It is more important in the early years for the children to understand the concepts involved than to be able to use some fancy notation they do not begin to comprehend.

Volume: Similarly, the units of volume are the cubic metre, cubic millimetre, cubic centimetre and cubic kilometre which should each be written m<sup>3</sup>, mm<sup>3</sup>, cm<sup>3</sup>, Km<sup>3</sup>, but in the early stages could be written cu.m, cu.mm, cu.cm and cu.Km respectively.

However, with volume there is a complication. Because the cubic millimetre and cubic centimetre are very small units of volume and the cubic metre is quite a large volume, we need something in between for everyday use. For this we use the litre. A litre is defined as the volume of a cube **10 cm x 10 cm x 10 cm**. Of course it does not always come in this shape. Orange juice cartons are often a litre in capacity but they are rarely cubic in shape. The symbol for the litre is simply the letter I, but this can cause confusion as it looks too much like the number one and so, although strictly speaking it is against the rules, it is sometimes better to write the full word. Some people like to use a capital letter L instead.

This definition means that there are **1000** litres in **1** cubic metre and **1000** cubic centimetres in **1** litre. Because 'milli' means 'one thousandth', a millilitre is therefore the same as a cubic centimetre. We tend to use millilitres for liquids and cubic centimetres for solids although they are really interchangeable (What happens when **500** millilitres of liquid water changes to ice?)

It is interesting and necessary to note that, although there are **10** millimetres in a centimetres, there are **100** square millimetres in a square centimetre.

Similarly, there are: 100 cm in 1 m, but 10 000 cm<sup> $^{2}$ </sup> in 1 square metre and 1 000 000 cm<sup> $^{3}$ </sup> in 1 cubic metre etc.

# Mass:

The basic unit of mass is the kilogram which is obviously **1000** grams. **1000** kilograms make a tonne. A kilogram is defined as the mass of one litre of water which turns out to be very useful as it follows that: One cubic metre of water (which is **1000** litres) has a mass of **1000** Kg (tonne). One cubic centimetre of water (which is 1 ml) has a mass of **1** g.

Abbreviations: You will notice that some abbreviations for the units begin with lower case letters whilst others begin with upper case letters.

The convention is that the fundamental units and subdivisions of them use lower case letters and multiples use upper case letters.

 $\mathbf{m}$ ,  $\mathbf{m}^2$ ,  $\mathbf{m}^3$ ,  $\mathbf{I}$  and  $\mathbf{g}$  are all basic units and so use lower case letters.

**mm, cm, m** (and their squares and cubes) are subdivisions of units so also use lowercase letters. **Km** and **Kg** are multiples of the basic units and so begin with capital letters.

Middle (R) The one between two others. This may refer to geometrical position such as a building that is in the middle of two other buildings. It may also refer to the middle of three or more values. Midnight (1) **12.00 p.m.** The dividing line between days. Children should realize that each day has a beginning and an end. Unfortunately this occurs when children are asleep. Or should be, I would say! Mile (3) An imperial unit approximately equal to **1.6 Km**. See the major topic on IMPERIAL UNITS. Millennium (4) One thousand years. Plural 'millennia'. See major topic TIME. Millilitre (2) One thousandth of a litre. See the major topic METRIC SYSTEM for more details. Millimetre (4) One thousandth of a metre. See the major topic METRIC SYSTEM for more details. Million (4) 1 000 000. One thousand thousands.  $10^6 = 10 \times 10 \times 10 \times 10 \times 10 \times 10$ . Minimum (5) The smallest of a set of values. This could refer to discrete data such as 'The minimum pocket money pupils should bring on the school trip is £10' or to continuous data such as 'What was the minimum temperature reached in the playground this afternoon?' Minus (1) The most confusing word in mathematics since it has two completely different meanings, but we mix the meanings up and even combine them willy nilly. The first meaning is 'negative', i.e. to indicate a number whose value is less than zero. Here it is used as an adjective. The second meaning is 'subtract' or 'take away'. Here it is used as a verb – an operation. In the early stages everything goes swimmingly because the two meanings are kept well apart: What is **17** minus **8**? (An operation or verb) The temperature is 4°C. It falls 10°C. What temperature is it now? (Ans. Minus 6°C) (An adjective) The problems arise at secondary level when we mix the two meanings in the same sentence: Find **5** – **12** Here we notice that before the number **12** are two minuses and it is not long before you hear teachers saying 'Two minuses make a plus'. They simply skip over the fact that the first 'minus' is a subtraction (verb) and the second 'minus' is a negative sign (adjective) and combine them without further ado to give a 'plus'. But is this a 'plus' meaning 'add' (verb) or a 'plus' meaning 'positive' (adjective). If it is a verb we have just combined a verb with an adjective to give a verb. If it is an adjective we have just combined a verb with an adjective to give an adjective. This must rate as one of the greatest loads of codswallop flourishing in the education system. Not only that, but children then extend the idea of 'two minuses make a plus' to situations where it does not apply such as: **5** + **12** = **17** (i.e. **positive 17**). Unfortunately, this mess cannot be sorted out in a short article such as this; it really needs the co-

operation of all teachers of mathematics, probably the world over!

We mention it here to warn you to be careful when using the word 'minus'. Despite what it may say in the Numeracy Strategy Document, it is better to stick to 'negative' and 'subtract' (or 'take away' for younger children) and to avoid the use of the word 'minus' wherever possible.



#### More/most expensive (3)

Comparison of the cost of two or more items. See COMPARATIVE AND SUPERLATIVE.

#### Morning (R)

The period of time between midnight and noon. a.m.

It is important for children to know that the day is divided into parts – morning, afternoon, evening etc. This should be constantly reinforced by good use of language with children from an early age.

# Most (R)

Greatest quantity, number or amount.

#### Most common (2)

The number or object that occurs the greatest number of times.

# Most popular (2)

The item that is chosen by the greatest number of people.

#### Movement (R)

An introduction to translations, rotations etc. These may be performed in P.E. lessons and translated to paper as mathematical ideas later.

# Multiple of (2)

The numbers in the times table. E.g. The multiples of 6 are 6, 12, 18, 24, ...

Х	1	2	3	4	5	6	7	8	9	10	
1	1	2	3	4	5	6	7	8	9	10	Multiples of 1
2	2	4	6	8	10	12	14	16	18	20	◄ Multiples of 2
3	3	6	9	12	15	18	21	24	27	30	<ul> <li>Multiples of 3</li> </ul>
4	4	8	12	16	20	24	28	32	36	40	etc.
5	5	10	15	20	25	30	35	40	45	50	
6	6	12	18	24	30	36	42	48	54	60	
7	7	14	21	28	35	42	49	56	63	70	
8	8	16	24	32	40	48	56	64	72	80	
9	9	18	27	36	45	54	63	72	81	90	
10	10	20	30	40	50	60	70	80	90	100	

# Multiplied by (2)

Added together a certain number of times. E.g. 'Six multiplied by three is eighteen'.

# Multiply (2)

The operation of repeated addition. **4 x 6** means add six lots of four together. This can be tedious with larger numbers so it is very important that children learn their tables as soon as they are able. The use of calculators is a brilliant innovation in many respects, but teachers should make sure that children do have many opportunities to practise multiplication tables as well as many other mental calculations.

# Narrow (R)

Not very wide.

# NE (4)

See COMPASS POINT.

# Near double (1)

This describes the situation where one number is almost, but perhaps not quite the double of another. E.g. **19** is a near double of **10**. This becomes very useful later with sums such as *'calculate* **55** + **56***'* Doubling **55** gives **110**, so **55** + **56** must be one more, *i.e.* **111**.



# Noitcarf numbers. You will not find Noitcarf Numbers in the Maths Curriculum (or any other sane document, come to that), but they provide such a wonderful April Fool's trick for year six mathematically able pupils that it would be a shame to miss them out.

First, give the children a little of the background to the numbers – Henri Noitcarf was born in Paris in **1767** and died in **1852**, aged **85**. Among his more notable achievements was the invention of Noitcarf Numbers ...... (embellish at will).

Secondly give the rules for Noitcarf numbers. Each Noitcarf Number consists of two parts which are written in square brackets separated by a comma. Square brackets are used so that Noitcarf Numbers are not mixed up with co-ordinates. Either part of a Noitcarf Number may be zero, negative or include a decimal, but these additions make life rather difficult, so stick to positive whole numbers, (unless, of course, you have a class of geniuses)

Examples of Noitcarf Numbers are therefore [2, 5] [12, 17] and [150, 250]. The rules for the four operations are as follows. Take two Noitcarf Numbers [a, b] and [c, d].

Addition and subtraction are similar:

Addition: **[a , b] + [c , d] = [ad + bc , bd]** E.g. **[3 , 4] + [2 , 5] = [3 x 5 + 4 x 2 , 4 x 5] = [15 + 8 , 20] = [23 , 20]** 

Subtraction: [a, b] – [c, d] = [ad – bc, bd] E.g. [4, 5] – [2, 3] = [4 x 3 – 5 x 2, 5 x 3] = [12 – 10, 15] = [2, 15]

Multiplication and division are similar:

Multiplication [a, b] x [c, d] = [ac, bd] E.g. [6, 9] x [3, 5] = [18, 45]

Division [a, b] ÷ [c, d] = [ad, bc] E.g. [10, 12] ÷ [4, 7] = [70, 48]

Two Noitcarf Numbers are equal if one can be changed into the other by multiplying both parts by the same number. E.g. [4, 5] = [12, 15] because  $[4 \times 3, 5 \times 3] = [12, 15]$ 

Thirdly, having explained the rules and illustrated with examples, give the children some of their own to do and explain that these are used by design engineers when designing cars, bridges, structures and manufacturing machines.

How much better if you have a friend, unknown to the children, who can be a visiting 'professor' from your local university.

Hopefully, it will be some while before one of your children realizes that Noitcarf is fraction spelt backwards! Have fun!

# None (R)

An introduction to the concept of zero. This could be the number of toys in a bag after all have been removed, the height of a bar on a bar chart or the number of integers between **21** and **22**.

# Noon (4)

12.00 a.m. The moment half way between 11.59 a.m. and 12.01 p.m. See '12-hour clock'.

# North (3)

See the major topic COMPASS POINT.

# North-east (4)

See the major topic COMPASS POINT.



MathSphere dictionary for teaching assistants
Octahedron (5) A three-dimensional shape with eight faces.
A regular octahedron has faces which are all equilateral triangles:
October (2) See the major topic TIME.
Odd (R) An odd number, i.e. 1, 3, 5, 7, 9, 11, 13, So called because if you try to make two equal towers from an odd number of bricks, there will always be an odd one left over.
Older (R) See the major topic COMPARATIVE and SUPERLATIVE.
Oldest (R) See the major topic COMPARATIVE and SUPERLATIVE.
Once (1) a) Describes the fact that something has only happened the one time. b) Part of the times tables as in 'Once seven is seven'.
One (R) The first positive whole number. Positive whole numbers are often called Natural Numbers, because these are believed to have been the first numbers used in mathematics.
Open (4) See 'Closed'.
Operation (1) A process performed on shapes or numbers.
Is that all? I was afraid it was going to be something much more medical!
Shape operations are such things as 'reflect', 'rotate' and 'translate'.
Number operations divide into two groups: Unary operations involving just one number such finding the square or square root of a number. Binary operations involving two numbers such as addition, subtraction, multiplication and division.
<b>Operation key</b> (6) One of the keys that performs an operation on a calculator. On a simple calculator they will be +, -, x and $\div$ and sometimes $$ and $x^2$ . On scientific calculators these will be extended to <b>sin</b> , <b>cos</b> , <b>log</b> etc.

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# Opposite (R)

On the other side of.

# Origin (4)

The point where the x-axis and the y-axis meet. The co-ordinates of the origin are (0, 0). In the early years only the first quadrant (top right hand corner) is used. Later, all four are used. See 'Co-ordinates'.

#### Ounce (6)

An imperial unit approximately equal to thirty grams. See the major topic IMPERIAL UNITS.

#### Outcome (5)

What happens in an experiment in probability. The actual outcome is what really happened in an experiment. The expected outcome is what you would expect to happen in an experiment and they are rarely the same. E.g. The expected outcome when you toss a normal dice sixty times is ten ones, ten twos, ten threes etc, but you would be very suspicious if you actually achieved that! The reason for using the expected outcome is so that we can forecast or predict in real situations with some sort of accuracy.

For example, if we discovered from tests on a small number of patients that a new drug cured about one third of the patients on whom it was tried, we could then estimate the number of people who would be cured if we tried it on the population at large.

# P.M. (3)

See '12-hour clock'

# Pair (R)

Two matching items such as gloves or shoes. Items described as a *'pair'* are not often identical (although they may be in the case of decorated plant pots, for example). Often one is a reflection of the other as with shoes and gloves. Some things are called a *'pair'*, even though they are not, such as a *'pair of trousers'*. These were originally two separate legs which were only later sewn together. Often things match in some other way such as a married couple.



# Parallel (5)

Straight lines which are the same distance apart throughout their length. Sometimes they are described as lines that never meet, but this definition only applies to lines in two dimensions such as those drawn on a piece of paper. It is possible to have lines in three dimensions that never meet but are not parallel (try it with two rulers).

# Parallelogram (6)

A quadrilateral with two pairs of equal opposite sides. See the major topic TWO DIMENSIONAL SHAPES.

# Part (2)

Related to fractions. A part is a fraction, so a fourth part of something is the same as a quarter.

# Partition (1)

The splitting of a number into its component parts, I.e. units, tens, hundreds etc.

E.g. 'Partition 367 into hundreds, tens and units – this gives 3 hundreds, 6 tens and 7 units.'

This idea is used when we place beads on an abacus to represent a number.



# Perpendicular (5)

At right angles to something else.

E.g. 'The telegraph poles are perpendicular to the pavement', 'The gymnast kept his arms perpendicular to his body throughout the roll'.

Pictogram (2)

A type of graph in which drawings are used to represent numbers.

E.g. In this pictogram showing the number of people travelling to work by bus, by car and on foot, each stick figure represents 100 people.

BUS	₽ ₽	}	Ŷ	6/
		-		

❣❣❣

CAR

# Pint (4)

A unit used to measure liquid, equal to approximately half a litre.

# Place (2)

See the major topic DECIMAL SYSTEM.

# Place value (2)

See the major topic DECIMAL SYSTEM.

# Plan (3)

Similar to a map, but generally used for smaller area such as individual streets or buildings. A plan is always seen from above and is sometimes referred to as a 'bird's eye view'.

# Plane (6)

A flat surface. Two-dimensional shapes are drawn in a plane.

# Plot (4)

Putting points on a grid: 'Plot the point (6,7) on the grid'.

Plus (1)

Add.

# Point (1)

The sharp bit.

# Polygon (4)

A closed two dimensional shape whose edges are straight. See the major topic TWO DIMENSIONAL SHAPES.

# Polyhedron (4)

A three dimensional shape whose faces are polygons. See the major topic THREE DIMENSIONAL SHAPES.

**Poor chance (5)** Indicating a low probability of happening: *'The horse called "Stewball" had a poor chance of winning the race.'* 

That's not surprising – he must be over **50** by now!

Positive (4)

See the major topic INTEGERS.

#### Possible (5)

An event that has a chance of happening, no matter how low the probability, as long as it is not zero.

#### Pound (Mass) (6)

An imperial unit used to measure mass. Approximately 500g. See the major topic IMPERIAL UNITS.

#### Pound sign (£) (2)

Used to represent the currency of the U.K. Others children should be familiar with are the Euro symbol and the dollar sign.

#### Predict (2)

The task of telling the outcome of an experiment based on some previous experience.

# Prime factor (6)

A prime number that divides exactly into another number. E.g. *What are the prime factors of* **20**<sup>'</sup>. First write down the factors of **20** (i.e. all the whole numbers that will divide into it): **1**, **2**, **4**, **5**, **10**, **20**. Of these **2** and **5** are prime numbers and therefore prime factors of **20**. (Reminder: 1 is not a prime number). We can write any number as the product of its prime factors. E.g. **20** = **2** x **2** x **5** or **2**<sup>2</sup> x **5**.

E.g. The prime factors of 420 are 2, 3, 5 and 7. We can write  $420 = 2 \times 2 \times 3 \times 5 \times 7$  or  $2^2 \times 3 \times 5 \times 7$ . E.g. The prime factors of 216 are 2 and 3. We can write  $216 = 2 \times 2 \times 2 \times 3 \times 3 \times 3$  or  $2^3 \times 3^3$ .

# Prime number (6)

'A whole number which cannot be divided by any other whole number other than **1** and itself'. An alternative definition is 'A whole number with exactly two factors', which explains why 1 is not a prime number.

The first few prime numbers are 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31 ...

Some interesting facts about prime numbers:

Apart from **2** and **3**, all prime numbers are one more or one less than a multiple of 6. Another way of expressing this is to write all the whole numbers in rows with six in a row, thus:

1	2	3	4	5	6
7	8	9	10	11	12
13	14	15	16	17	18
19	20	21	22	23	24
25	26	27	28	29	30
		•			•

The prime numbers (except 2 and 3) are all in the first and fifth columns. As the sixth column is the multiples of six, the primes must be one more or one less than a multiple of six. It is easy to see why they are not in the other columns – columns 2, 4 and 6 are the even numbers, column 3 is the multiples of three. Make sure your children understand that this does <u>not</u> mean that <u>all</u> numbers in columns 1 and 5 are prime numbers e.g. 5 and 25 are not prime.

The largest known prime number before computers started to work on the problem was  $2^{127} - 1$ , which is: 170 141 183 460 469 231 731 687 303 715 884 105 727 discovered by Lucas in 1876!





#### Quadrant (5)

One of the four areas of the co-ordinate grid. The top right area is known as the first quadrant, the top left the second quadrant and so on anti-clockwise. See 'Co-ordinates' for diagram.

#### Quadrilateral (3)

A two dimensional shape with four straight sides. See the major topic TWO DIMENSIONAL SHAPES.

# Quarter past (2)

This should be associated with a quarter turn of the big hand, reinforcing several ideas: a complete rotation of the big hand represents one hour, a quarter turn is a right angle, the hands move clockwise and that the quarter hour is independent of the position of the small (hour) hand.

# Quarter to (2)

As above, but with the difference that 'quarter to' is represented by three-quarters of a full turn.

# Quarter turn (2)

A turn of one right angle (**90**<sup>0</sup>).

# Questionnaire (4)

A group of questions designed to collect data that may be used to give the answer to an important question through finding averages, drawing graphs etc. The most important thing about a questionnaire is that it should have a specific purpose. In other words, the collected data should be able to help the pupils answer specific questions into research they are conducting, so they should have a clear idea of what it is they are trying to find out.

Obviously, in the early years, this will be something simple such as finding the favourite chocolate bar of the class, as we are mainly interested in teaching the children how to process the data, but later it should develop into something more worthwhile such as supporting a project to develop the school play facilities or how the local parks are used throughout the four seasons of the year. In order to design the questionnaire, the children should know what data needs to be collected to answer their questions and what graphs and statistics they will need. This should then lead to a questionnaire that is purposeful in that it collects the necessary data. In other words, the questions are generally the last items to be written – a good plan of what is required is the first item to be constructed.

#### Quicker (R)

See the major topic COMPARATIVE and SUPERLATIVE.

#### Quickest (R)

See the major topic COMPARATIVE and SUPERLATIVE.

# Quotient (4)

The answer when one number is divided by another. E.g. 'The quotient of 12 and 4 is 3'.

#### Radius (4)

The line or distance from the centre of a circle to any point on the circumference.

# Random (6)

A number chosen without any bias in its choosing. This can be achieved for all practical purposes with a physical device such as a dice or spinner. Surprisingly, it is very difficult to achieve this with software and random number generating programs on computers often have a slight bias towards certain numbers, although this is hard to detect.

#### Range (5)

The difference between the largest and the smallest of a set of numbers. E.g. 'The range of these numbers 3, 13, 32, 5, 15, 6, 19 is 32 - 3 = 29'. It is not correct in mathematics to say that the range is from 3 to 32, although this is often done in other subjects as in 'The temperature range was from  $10^{\circ}C$  to  $22^{\circ}C$ .'

# Record (1)

The making of a permanent statement of the results of calculations, experiments etc. This may be in the form of a written statement, graph, audio/video tape etc.

# Rectangle (R)

A quadrilateral with two pairs of parallel sides and four right angles. See the major topic TWO DIMENSIONAL SHAPES.

Rectangular (2)

In the shape of a rectangle.

# Recurring (6)

Decimal numbers come in three types:

a) those that finish after a certain number of decimal places such as **5.873524363363** 

b) those that extend to the right for ever with a repeating pattern such as **98.8989898989898989**...

c) those that extend to the right for ever but do not repeat such as  $\pi$  = 3.14159265358979323846... and  $\sqrt{2}$  = 1. 41421356237309504880...

Type b) are called recurring decimals. There are two ways of obtaining them. The first is to simply make them up. Choose a number of digits and simply repeat them. The second is to perform certain division sums. Bearing in mind that fractions can be thought of as division sums (see the major topic on FRACTIONS), this translates into changing a fraction into a decimal, choosing the numerator and denominator carefully.

E.g. dividing by **3**, **7**, **9**, **11** etc and their multiples such as **6**, **21** and **45** will generally give recurring decimals provided that the number into which you are dividing is not a multiple of the divisor.

So,  ${}^{1}/_{3} = 1 \div 3 = 0.3333333...$   ${}^{2}/_{3} = 2 \div 3 = 0.66666666...$   ${}^{2}/_{7} = 2 \div 7 = 0.285714285714285714285714...$ 

To begin with children will only come across simple recurring decimals such **0.333333**... and **0.6666666**..., but quite quickly those who love to play with numbers can start to explore all sorts of patterns.

E.g. Divide each of the numbers 1, 2, 3, 4, 5 and 6 by 7 in turn and look for patterns.

Try changing recurring decimals back to fractions. This can be done (we do not have space to explain why this works here) by taking one set of the recurring digits and making them the numerator of a fraction. The denominator is them made up from the same number of nines.

E.g. Change **0.333333...** to a fraction. We see only one digit is repeated (**3**) and so all we need to do is put this as a numerator with one nine as a denominator:  ${}^{3}/_{9}$ . This can, of course, be cancelled to  ${}^{1}/_{3}$ , giving the fraction that is usually associated with **0.333333...** (There are others, of course, such as  ${}^{2}/_{6}$ ,  ${}^{5}/_{15}$  and so on, but these are simply fractions that are equivalent to  ${}^{1}/_{3}$ .)

E.g. Change **0.153153153...** to a fraction. We notice that this time there are three recurring digits (**153**) and so we put these as the numerator with three nines as the denominator:  ${}^{153}/_{999}$ . After a little thought, we notice that this fraction will cancel by nine (the digits **153** add to **9** and so **153** is divisible by **9**). Cancelling gives  ${}^{17}/_{111}$  which is a fraction in its lowest terms. Dividing **17** by **111** on a calculator confirms this fraction is indeed **0.153153153...** 

Recurring decimals can sometimes need some hard thought on the part of the children. For example, swimming three lengths of a pool that is  $33^{1}/_{3}$  metres long gives a distance of **100m**. But  $33^{1}/_{3}$  is **33.333333...**, so three lengths must be **99.999999...**m. Is the swimming test complete? (This, of course, proves that **99.9999999...** is the same as **100**, but children need to think about this quite a bit before accepting it).

One last thing. There is an abbreviation for recurring decimals. There is no need to write the recurring digits out several times. Simply put a dot over the first and last of the recurring digits (or just the recurring

digit if there is just one). So 0.247424742474... can be written:

0.2474

Some recurring decimals have non-recurring digits immediately after the decimal point followed by the recurring digits. E.g.  ${}^{67}I_{90}$  gives **0.744444...** and  ${}^{8007}I_{11100}$  gives **0.72135135135...** which can be written

•			
0.74	and	0.72135	respectively.

# Reduced to (5)

A term used when dealing with equivalent fractions to express the fact that the fraction has been cancelled to something simpler. E.g. ' $^{50}/_{60}$  can be reduced to  $^{5}/_{6.}$ ' E.g.  $^{7}/_{11}$  is a fraction that has been reduced to its lowest terms.'

#### Reflection (2)

What you see when you look in a mirror. This idea is then extended to 'mathematical' mirrors. The difference between a normal mirror and a mathematical one is that with a normal mirror you can only stand in front of it to see a reflection. With a mathematical mirror, you can stand either side and see a reflection. This idea is used to describe shapes that have reflective symmetry in that the left side can be reflected to the right side and the right side can be reflected to the left side. If, therefore, we are given only one side of a shape that we know has reflective symmetry, we can draw the other half, no matter which side it is on.



# MathSphere dictionary for teaching assistants Repeating pattern (R) A repeating pattern can be very simple such as the repeating of coloured squares (red, blue, green, red, blue, green...) or it can be more complex perhaps involving reflected or rotated shapes. This gives children an introduction to more complex problems on reflections and rotations they will meet later in life. Represents (2) When one item represents another. A £1 note, for instance, represents 100 pennies. A step on a block graph could represent five people or things or in place value the third digit to the left of the decimal point represents hundreds. Rhombus (6) A quadrilateral with four equal sides. See the major topic TWO DIMENSIONAL SHAPES. Right (R) Correct. Children should enjoy learning and it is essential that they are not criticized too much for mistakes they make, which are a natural part of the learning process ('to err is human'). Children love to be told that they have something correct, but feel bad when their answers are wrong, so try to avoid using this word if possible. The most important thing to do if a mistake is made is to use a less critical phrase such as 'not quite correct' and then make an effort to see where they have gone wrong and help the child to understand his/her mistake. Too many children say 'I'm not very good at maths' when they are only seven or eight years old. This is guite an indictment on the skills (or lack of) of some teachers. This is not to say that children should not sometimes be reprimanded for lack of effort or concentration, which is a different matter. I had a teacher once who asked my name in a maths lesson. When I said, 'Divvy', he said, 'Yes. that's right!' Right angle (2) A quarter turn or **90**°. **Right-angled (3)** Containing a right angle (as in right-angled triangle). Risk (5) Used to assess the probability of something happening as in, 'If I stay late at school this afternoon, there is a high risk I will miss my bus.' Roll (R)

Used to describe the property that some objects will roll whilst others will not.



# Round (R)

Used to describe the circular nature of an object: 'Footballs are round.'

# Round to the nearest hundred (4)

Giving a number to the nearest hundred: 'Round **475** to the nearest hundred.' See ROUND.

# Round to the nearest ten (2)

Giving a number to the nearest ten: 'Round 87 to the nearest ten.' See ROUND.

# Rounding (5)

The process of giving a number to a pre-defined accuracy. For examples see ROUND.

# Route (2)

A way from place A to place B on a simple map. Normally given as a series of instructions or a line drawn on a map.



It's a good idea for children to have some understanding of how the Global Positioning Satellite System is used to track vehicles and help drivers find the route to their destination.

#### Row (2)

Rows and columns as used in an array such as a table square. Columns run from top to bottom like the columns in the old Greek or Roman buildings; rows run from left to right as do the seats in a cinema.

# Ruler (1)

Rulers used by young children will show only centimetres, but millimetres will be included as soon as they are able to manage these. However, in the same way that small hands need big bricks, young minds need big units and it is a mistake to introduce millimetres too early. What is important is to practise the process of measuring which is never as simple as it seems. See *'Measure'* for a discussion of this point.

# Saturday (2)

See the major topic TIME.

# Scalene triangle (5)

A triangle with no special properties i.e. all its sides are different lengths. See the major topic TWO DIMENSIONAL SHAPES.

#### Scales (R)

See 'Weigh'.

# Score (R)

A result obtained in a game such as darts and some card games.

**SE** (4)

See COMPASS POINT.

#### Seasons (1)

The important thing about seasons is that they are cyclic like the days of the week and the months of the year. They always come in the same sequence, but there was no first season and there will be no last.

TIME for more in Second (R) See the major to	r it is combined with other units such as distance to produce speed. See the major topic formation.
Semi-circle (3) A half circle:	
	Open Closed
September (2) See the major to	pic TIME.
b) A set of number E.g. 2, 4, 6, 8, E.g. 6, 3, 0, -3 E.g. 2, 5, 4, 7, Some pattern going up and third example	ers written in a logical sequence 10, 12, 14, , -6, -9, 6, 9, 8, 11, 10 (add 3, subtract 1) ns alternate between d going down as in the e.
Set (R) A group of items	or numbers that are related. See also 'Venn and Carroll Diagrams'.

Set square (4)						
A triangular piece of plastic shaped to have either a) one right angle and two <b>45°</b> angles or b) one right angle, a <b>30°</b> angle and a <b>60°</b> angle.						
60 <sup>0</sup> 30 <sup>0</sup>		45 <sup>0</sup>				
₹90°	<sup>ر</sup> 90°					
60º/30º Set Square	4	5 <sup>0</sup> Set Square				
Share equally (2) Introduction to division.						
Shorter (R) See the major topic COMPARATIV	E and SUPERLATIVE.					
Shortest (R) See the major topic COMPARATIV	E and SUPERLATIVE.					
Side (R) One of the edges joining two corne	ide (R) One of the edges joining two corners on a polygon.					
Sign (1) Initially the equals, add, subtract, multiply and divide signs, but later the negative and square root signs etc.						
Sign change (6) A key on a calculator that changes negative and visa versa.	the sign of the number in the d	splay. If it was positive, it becomes				
Sixth (4) a) See the major topic CARDINAL b) One sixth as a fraction: <sup>1</sup> / <sub>6</sub> . One	and ORDINAL NUMBERS. whole divided by six.					
Sketch (4) A reasonable accurate drawing of a accurately to scale.	n object or shape, showing the	essential features but not drawn				
Slower (R) See the major topic COMPARATIV	E and SUPERLATIVE.					
Slowest (R) See the major topic COMPARATIV	E and SUPERLATIVE.					
Smaller (R) See the major topic COMPARATIV	E and SUPERLATIVE.					

# Smallest (R)

See the major topic COMPARATIVE and SUPERLATIVE.

# Sold (2)

Past tense of 'sell'.

# Solid (R)

Used to refer to a shape that has no empty space inside – opposite of 'hollow'.

#### Sort (4)

An instruction to classify shapes or numbers by their properties. E.g. 'Sort these numbers into prime and non-primes', 'Sort these shapes according to how many right angles they have'.

# South (3)

See the major topic COMPASS POINT.

# South-east (4)

See the major topic COMPASS POINT.

# South-west (4)

See the major topic COMPASS POINT.

#### Sphere (R)

A ball shape. More technically, a three dimensional shape for which every point on its surface is the same distance from a fixed point (the centre).

# Spherical (4)

In the shape of a sphere. 'Most planets are spherical in shape.'

#### Spinner (5)

A device that can be spun to generate a random number. Used in the study of probability. One type is made from a piece of plastic or card in the shape of a regular hexagon, octagon etc on which numbers are written. It then has a rod through the centre so that it may be spun, rather like a small gyroscope.



Spring (1)

One of the four seasons. The main idea for children to understand is that the seasons are cyclic, without beginning or end.

Square (R)

- a) A quadrilateral with four equal sides and four right angles. See the major topic TWO DIMENSIONAL SHAPES.
- b) Non-Daddyo.

# Square centimetre (cm<sup>2</sup>) (4)

The area of a square **1cm x 1cm**. See the major topic METRIC SYSTEM.

Square metre (m<sup>2</sup>) (5)

The area of a square **1m x 1m**. See the major topic METRIC SYSTEM.

Square millimetre (mm <sup>2</sup> ) (5)
The area of a square <b>1mm x 1mm</b> . See the major topic METRIC SYSTEM.
Square number (5)
A number that results from multiplying an integer by itself. E.g. 9 is a square number because it results
from <b>3 x 3</b> . These numbers are called 'square' because they can be drawn in the shape of a square array:
0 0 0
$\odot$ $\odot$ $\odot$
The first few square numbers are 0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100
Square-based (1)
A three dimensional shape that sits on a square face known as its base. This is normally used to refer to
pyramids. <i>'The Egyptian pyramids are all square-based pyramids'</i> . See the major topic THREE DIMENSIONAL SHAPES.
Standard unit (4)
When children begin measuring they can use any convenient unit such as hand spans or strides. Pretty
soon, however, with a little encouragement from their teacher, they feel the need to have a standard unit
so that people agree on the length or mass of an object. Standard units such as metre, centimetre and
kilogram are normally amongst the first to be introduced.
Stands for (2)
A reference to place value. E.g. 'The second digit from the right (or from the decimal point) represents
tens.'
Star (R)
Simply refers to a star shape. Later, the reflective and rotational symmetry of star shapes can be
discussed.
Statistics (6)
I he study of collecting and analyzing data. Includes collecting data through surveys, graph drawing, and
finding averages.
Straight (line) (R)
I he idea of a straight line. The shortest distance between two points. Polygons are made from straight
lines and so on.



Stretch (R)
example.
What, like this?
And the first the second
Subtract (1) The process of taking one number from another. There are many ways of subtracting such as counting on; counting back; counting up to the next ten, then between tens and finally to the second number; decomposition.
Sum (R)
<ul> <li>This term has two meanings:</li> <li>a) Any operation that involves addition, subtraction, multiplication or division.</li> <li>b) The stricter definition of the answer to an addition sum. E.g. <i>'The sum of six and five is eleven.'</i></li> </ul>
Summer (1)
One of the four seasons. The main idea for children to understand is that the seasons are cyclic, without beginning or end.
Sunday (2) See the major topic TIME.
Surface (2) A portion of space having length and breadth but no thickness. One of the faces of a three-dimensional shape. The area of a surface is often required to be found. See AREA.
Survey (4) The collection of data, normally by going out into the field with questionnaires.
SW (4) See COMPASS POINT.
Symbol (2)
Any character that represents some concept. For example, road signs represent road works etc, figures represent numbers, flags represent countries. Given that figures (themselves an abstract concept) represent the abstract concept of number, it is surprising that children catch on so quickly when learning to count and to write numbers.
Symmetrical (R) A shape may have reflective or rotational symmetry and is therefore described as <i>'symmetrical'</i> .
Taller (R)         See the major topic COMPARATIVE and SUPERLATIVE.
Tallest (R)           See the major topic COMPARATIVE and SUPERLATIVE.
<b>Tally</b> (2) A method or recording counting in which a line is drawn for each number counted. These are drawn in groups of five with the first four vertical and the fifth horizontal.
E.g. This tally represents 23:






Note that pyramids and cones are not prisms because, although they have the same cross sectional shape throughout their length (or height), this changes in size as we move along the axis of the pyramid or cone.



### Thursday (2)

See the major topic TIME.

## TIME (R)

There are many aspects to the subject of time which children must learn as they progress through school.

Firstly, there are the ways we divide up time and the labels we use to discuss it. We refer to the following:

<u>Millennia</u>: a millennium is a thousand years and on our calendar normally starts at a complete multiple of **1000** plus **1** year, **1-1000** being the first millennium, **1001-2000** the second millennium, **2001-3000** the third millennium and so on. Notice that although the millennia begin on years **1**, **1001**, **2001** etc, we celebrated the new millennium in the year **2000** because celebration is more to do with round numbers than it is with technical accuracy!

<u>Centuries</u>: a century is a hundred years and on our calendar normally starts at a complete multiple of **100** plus **1** year, **1-100** being the first century, ..... **1901-2000** the twentieth century, **2001-2100** the twenty-first century and so on.

<u>Years</u>: a year is the time it takes the Earth to orbit once about the Sun. This time is just under **365**<sup>1</sup>/<sub>4</sub> days. As we like days to begin at midnight, we deal with the extra quarter days by introducing leap days every four years on February **29**<sup>th</sup>. Unfortunately, because the orbital period is slightly under **365**<sup>1</sup>/<sub>4</sub> days, this means we have too many leap years. The solution is that every fourth year in the calendar is a leap year unless it is divisible by **100**. However, every **400**<sup>th</sup> year **is** a leap year.

The following are therefore leap years: **1600**, ... **1980** ....**1996**, **2000**, **2004**, ... **2020**,... **2400** etc The following are not leap years: **1700**, **1800**, **1900**, **2100**, **2200**, **2300**, **2500** etc It is interesting to note that not all calendars in the world begin at midnight on January 1<sup>st</sup>. A calendar commonly used in the east begins its year at the precise moment of the Spring Equinox on or about **21**<sup>st</sup> March!

<u>Months</u>: Children need to learn the names and order of the months of the year as well as the number of days in each. It is also a good idea for them to learn how to spell them: January **31** February **28/29** March **31** April **30** May **31** June **30** July **31** August **31** September **30** October **31** November **30** December **31** 

It helps children realize the significance of months if they use a calendar and put on it any significant days in their lives – Christmas Day, birthdays of themselves and their friends, beginning and end of school terms etc.

<u>Weeks</u>: There are, of course, fifty two weeks in a year, each with seven days. This gives **364** days in all. Hence we have a surplus of one day each year (two in leap years). That is why a fixed day (your birthday, for example) moves forward one day of the week each year (two days where there is February **29**<sup>th</sup> in between). If your birthday was on a Wednesday in **2002**, it would have been on a Thursday in **2003**.

<u>Days, Hours, Minutes, Seconds</u>: Children need to know there are **24** hours in a day, **60** minutes in an hour and **60** seconds in a minute. As they grow older it is also useful to know that there are **3600** seconds in an hour and **84 600** seconds in a day.

As a matter of interest a million seconds is **11** days, **13** hours, **46** minutes and **40** seconds and A billion seconds is approximately **31** years and **251** days, depending on leap years. So someone born at midnight on **1**<sup>st</sup> January **2000** will pass the one billion second mark at **1** hr **46** min and **40** seconds past midnight on **1**<sup>st</sup> June **2031**.

Secondly, children need to know in year six the difference between Greenwich Mean Time and British Summer Time. Greenwich Mean Time can be thought of as 'Sun time'. It is the time at which the Sun is due south at midday. Because the Earth does not orbit the Sun in a perfect circle and because we divide the Earth's surface into time zones in which quite a large part of the Earth has the same time regardless of its geographical location within that time zone, the Sun is not often exactly south at midday, but it is a good approximation that suffices for everyday use. (If you live in Eastern England and travel to the west coast of Ireland, for example, you will notice how much later, according to your watch, the sun sets in the evening). It's also interesting to note that despite its great size, there is only one time zone in China. Greenwich Mean Time (**G.M.T.**) is also known as Universal Time (**U.T.**), particularly by astronomers, and Zulu Time (**Z.T.**).

British Summer Time is simply Greenwich Mean Time with one hour added on. The clocks go forward at **1 a.m. G.M.T**. on the last Sunday in March and back at **1 a.m. G.M.T**. on the last Sunday in October. If you cannot remember which way to set your clocks simply remember 'Spring forward, fall back' (fall = autumn). We do this so that in the summer everyone goes about their daily business one hour earlier and arrives home one earlier than in winter so that they may enjoy the longer summer evenings at home instead of in the office/school etc.

Thirdly, there are the ways we record the passage of time. We can do this over longer periods of time by marking dates in a diary, calculating the time between two dates and placing historical events on a time line.

Over shorter periods we can record the time in seconds and minutes using stop watches/clocks or timers connected to computers. There is even a set of plastic shapes that rock back and forth for a given time (say, ten seconds). As we use time so much in our modern society, children should be given every opportunity to record the time taken to perform certain tasks: travelling from home to school, counting to one hundred, saying the eight times tables and so on. This also gives sets of data that may be used for drawing graphs, finding averages etc.

Fourthly, children should be familiar with timetables. These can be as simple or as complicated as one wishes. Children can begin by making their own timetable of the things they do in a day and progress to but and train timetables.

Fifthly, there is the use that is made of time when it is combined with other units. The most obvious example of this is that of calculating speed, which is time combined with distance. There are numerous experiments children can perform in which they time how long it takes them to run **100** metres and calculate their average speed. The same experiments can be conducted for cyclists, motorists, snails – the world is your oyster!

There also many other units with which time can be combined such as litres in calculating how much water flows along a stream/pipe or into a bath per second, how many grapes can be eaten in a minute, how many degrees the temperature of a kettle of water rises per minute, how many kilograms of sand can be shoveled into empty buckets per minute, how many milliliters of orange juice can be sucked through a straw per second (time over a ten second period and divide by ten).

### Timer (2)

A device for measuring time. This may be a clock, watch, stopwatch, water timer, sand timer or any other suitable device.

### Times as big as, as long as, as wide as etc (2)

Indicates number of times one thing is as big/long/wide etc as another. E.g. 'The classroom is six times as long as that table'.

# Timetable (4)

A chart showing times of trains, buses etc or lessons in school.

#### Title (2)

Every graph or chart should have a title and children should be encouraged to provide one at every opportunity. They should be learning that, although the purpose of the graph or chart is clear to them, it may not be clear to others and need explaining.

### To every (5)

Used when describing patterns. E.g. 'To every square there are four circles'.

### Today (R)

See the major topic TIME.

### Tomorrow (R)

See the major topic TIME.

### Tonne (6)

One thousand kilograms. See the major topic METRIC SYSTEM for more details.

#### Total (R)

The sum of a set of numbers. Used in various situations such finding the average (mean) and finding a total cost of a shopping list.

### Translation (4)

A slide in a particular direction. Later this can be executed on a squared board such as translating a shape three squares to the right and one up.

#### Trapezium (6)

A quadrilateral with one pair of parallel sides. See the major topic TWO DIMENSIONAL SHAPES.

### Triangle (R)

A two dimensional shape with three straight sides. See the major topic TWO DIMENSIONAL SHAPES for the different types.

### Triangular (2)

In the shape of a triangular. E.g. 'That box of chocolates is triangular in shape.'

# Tuesday (2)

See the major topic TIME.

#### Turn (R)

A complete rotation, i.e. **360<sup>°</sup>**. May be subdivided as in half-turn, quarter turn etc.

#### Twentieth (4)

- a) See the major topic CARDINAL and ORDINAL NUMBERS.
- b) One twentieth as a fraction:  $1/_{20}$ . One whole divided by twenty.

### Twenty-second (2)

See the major topic CARDINAL and ORDINAL NUMBERS.

## Twenty-first (2)

See the major topic CARDINAL and ORDINAL NUMBERS.

### Twice (1)

Two times.

#### Two hundred (2)

See the major topic on the DECIMAL SYSTEM.

### Two, three etc (R)

See the major topic on the DECIMAL SYSTEM.

#### **Two-dimensional** (4)

Having only length and width, but no thickness. Although it is not strictly correct, we sometimes think of the surface of an object such as a sphere or cylinder as two-dimensional as it allows us to illustrate some very interesting geometric possibilities such as two-dimensional creatures living on the surface of a sphere.

# TWO DIMENSIONAL SHAPES

Shapes that have length and width but no thickness. In other words, shapes that can be drawn on a piece of paper. There are, of course, an infinite number of such shapes but some are more interesting from a mathematical point of view than others:

Most of the interesting shapes are made up from straight lines, the circle being a notable exception. The main classification we can therefore make is by the number of sides:

Triangles (3 sides). The basic types of triangle are:









**Isosceles:** Two equal Sides **Equilateral:** Three equal Sides Right angled: One right angle **Obtuse angled:** One obtuse angle Scalene: No sides equal

The scalene triangle is very unusual in that is probably the only shape defined as having no special properties. Normally in mathematics, we define objects by the properties they have, not by the ones they do not have.

With triangles, equal length sides means equal angles, so the isosceles triangle has two equal angles and the equilateral triangle has three equal angles.

Quadrilaterals (4 sides). The basic types of quadrilaterals are:





# Units boundary (5)

In the same way as when we go from, say, **49** to **61**, we cross the tens boundary, we cross the units boundary when we go from, say, **8.9** to **9.1**.

### Unlikely (5)

Used to describe the idea that some events are not very likely to happen, i.e. they have a low probability of happening. E.g. *'If I toss a coin ten times, it is unlikely that I will obtain ten heads.'* 

### Usually (1)

The idea that some things are more likely to happen and therefore have a higher probability than others. E.g. *'My mother usually meets me after school.'* 

### Value (3)

a) The idea that objects have an intrinsic value and may be exchanged for others according to this value. Included in this is the idea that money has value which is not necessarily related to the number of coins/notes we have.

b) The idea that a digit can have a different value depending on its place in a number. See the major topic PLACE VALUE.

# Venn and Carroll Diagrams (3)

Two types of diagram used for sorting numbers or objects.

Numbers with 2 tens



	Carroll Diagram	
Odd Nos.	23 25	31 55 71
Non-odd Nos.	26 38	32 46
	Nos. with	Nos. <u>not</u>

two tens. with Two tens

Here, the numbers 23, 25, 26, 31, 32, 38, 46, 55 and 71 have been sorted in both types of diagram.

# Vertex (3)

Odd numbers

A 'corner' on a two or three dimensional shape; the point at which two or more edges meet. See the major topic THREE DIMENSIONAL SHAPES.

# Vertical (3)

At right angles to the Earth's surface locally.

# Vertices (3)

Plural of 'vertex'.

# Vote (1)

A way of collecting data. Voting for your favourite chocolate bar so that a block graph may be drawn.

# Watch (R)

See the major topic TIME.

# Wednesday (2)

See the major topic TIME.

# Week (R)

See the major topic TIME.

# Weekend (1)

The two days Saturday and Sunday taken together.

# Weigh (R)

The process of finding the weight or mass of an object. (If you are not sure of the difference see the major topic MASS and WEIGHT). In the early stages it is enough to show that some objects weight more than others. Objects may be compared by putting each in one pan of a balance:



Later standard weights can be put in one pan to balance an object whose mass is unknown. By making the balance level we can find the mass of the unknown object.

It is interesting to note that this method of finding the mass of an object will work on any planet because the reduction in gravitational force affects each pan equally.

Later, mass may be found by using a weighing scale with a rotating needle such as the type used to measure our own body weights or the older type of Post Office scales. These days many are digital, but whether analogue or digital, they both make use of a spring against which the weight of the object presses. This type would give a different reading of mass because the force pushing against the spring depends on the force of gravity.

## Weighs (R)

Used to indicate the weight (or mass – see discussion in major topic MASS and WEIGHT) of an object: 'The book weighs **400 g**.'

# Weight (R)

See the major topic MASS and WEIGHT.

### West (3)

See the major topic COMPASS POINTS.

# Whole turn (1)

A turn of 360°.

Children can begin to appreciate a whole turn by rotating their bodies about a vertical axis so that they finish facing the same way as they started. They can do this in the classroom or in P.E. lessons.

They can be asked to rotate two or three whole turns without stopping, but emphasize precision – you don't want them getting dizzy and falling over! They can also be asked to rotate their heads by a whole turn without moving their bodies to show this particular rotation is not always possible. They can then rotate both two and three dimensional objects a given number of times both clockwise and anti-clockwise.

Later they will come to appreciate that a rotation has a centre – a point that remains in the same place during the rotation. This may be inside the shape or outside as illustrated below:

Left: Shape is being rotated about a point Inside the shape.	Right: Shape is being rotated about a point Outside the shape.		
Winter (1)			
One of the four seasons. The main idea for children to understand is that the seasons are cyclic, without beginning or end.			
<b>x-axis</b> (5) The horizontal axis on a graph is normally labelled 'x' when no other label (such as 'time') is appropriate or when working with equations of the form $y = 4x - 6$ .			
Yard (6) An imperial measure just short of a metre. See 'Imperial Units'.			
<b>y-axis</b> (5) The vertical axis on a graph is normally labelled 'y' when no other label (such as 'frequency') is appropriate or when working with equations of the form $y = 4x - 6$ .			
Year (1) See the major topic TIME.			
Yesterday (R) It is important for children to realize that today does not stand in isolation. There are days before it and days after it. Yesterday's tomorrow is tomorrow's yesterday!			
<ul> <li>Zero (R)</li> <li>A number dividing the negative numbers from the positive numbers and is therefore neither positive nor negative itself. See the major topic INTEGERS for more information. It is interesting to understand that this number had to be invented to enable us to answer question such as:</li> <li><i>What is</i> 7 <i>subtract</i> 7 ?'</li> <li><i>A farmer had</i> 23 <i>sheep. They all died from a disease. How many did he have left?</i></li> <li><i>How many numbers are there that are both prime numbers and multiples of</i> 3?</li> </ul>			